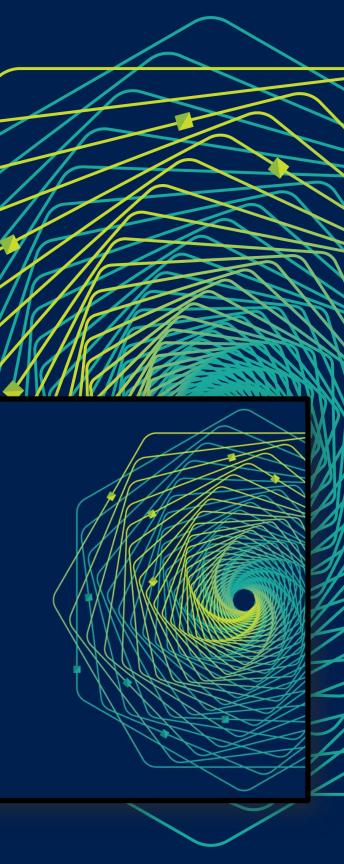


An HPC Systems Guy's View of Quantum Computing

Torsten Hoefler ETH Zurich, Switzerland (Professor) Microsoft Quantum, Redmond (Visiting Researcher)



Who is this guy and what is he doing here?

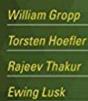




1 professor, 6 scientific staff, 13 PhD students

ETHzürich

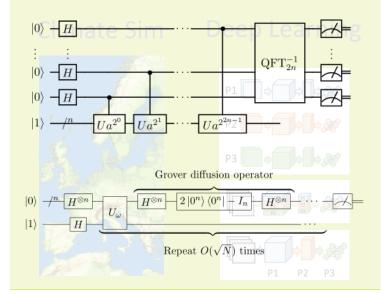
6.5k staff, 20k students, focus on research



ENGINEERS.

SPRING

Applications



Programming Systems

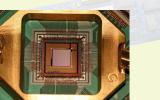


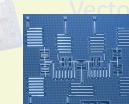
L|QUi|>



Accelerator Hardware



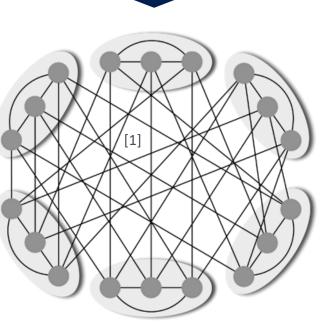




[1] M. Besta, TH: Slim Fly: A Cost Effective Low-Diameter Network Topology, IEEE/ACM SC14, best student paper



Message-Passing Interface



What is a qubit and how do I get one?

"I don't like it, and I'm sorry I ever had anything to do with it." Schrödinger (about the probability interpretation of quantum mechanics)

$$|\Psi\rangle = \alpha_0 | \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} + \alpha_1 | \begin{pmatrix} 0 \\ 1 \end{pmatrix} | \alpha_0 |^2 + |\alpha_1|^2 = 1$$

For example:
$$|+\rangle = \frac{1}{\sqrt{2}} |0\rangle + \frac{1}{\sqrt{2}} |1\rangle$$

One qubit can include a lot of information in α_0 and α_1 but can only sample one bit while losing all

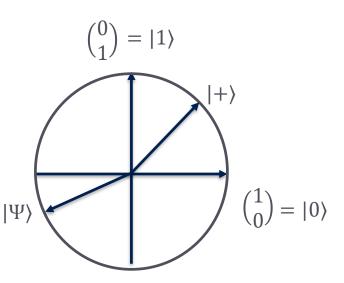
(encoding n bits takes $\Omega(n)$ operations)



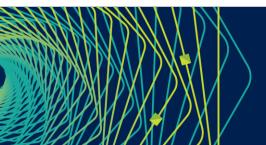
n qubits live in a vector space of 2^n complex numbers (all combinations + entanglement)

$$|\Psi_{n}\rangle = \sum_{i=0..2^{n}-1} \alpha_{i}|i\rangle$$
 e.g., $|\Psi_{2}\rangle = \alpha_{0}|00\rangle + \alpha_{1}|01\rangle$

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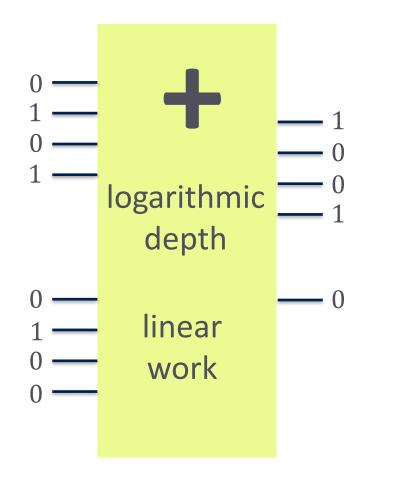


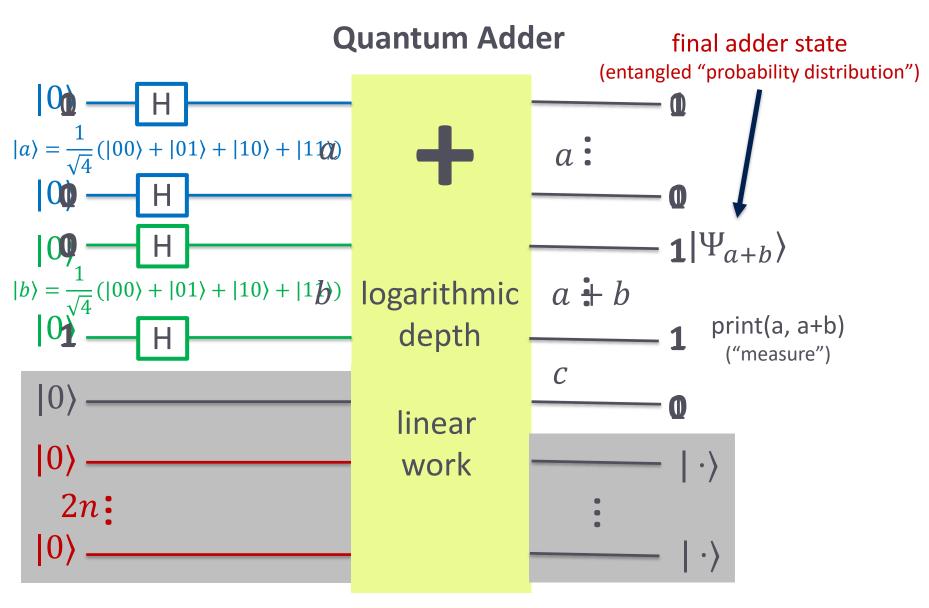
$+ \alpha_2 |10\rangle + \alpha_3 |11\rangle$

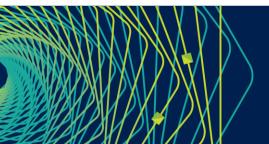


Example: adding 2^n numbers in $O(\log n)$ time









Example: adding 2^n numbers in $O(\log n)$ cycles We add all 2ⁿnumbers in parallel but only recover n classical bits!

A Corollary to Holevo's Theorem (1973): *at most n classical bits can be* extracted from a quantum state with n qubits even though that system requires $2^n - 1$ complex numbers to be represented!

My corollary: practical quantum algorithms read a linear-size input and modify an exponential-size quantum state such that the correct (polynomial size) output is likely to be measured.

Question: Are quantum algorithms good at solving problems where a solution is verifiable efficiently (polynomial time)? Answer: Kind of *©*



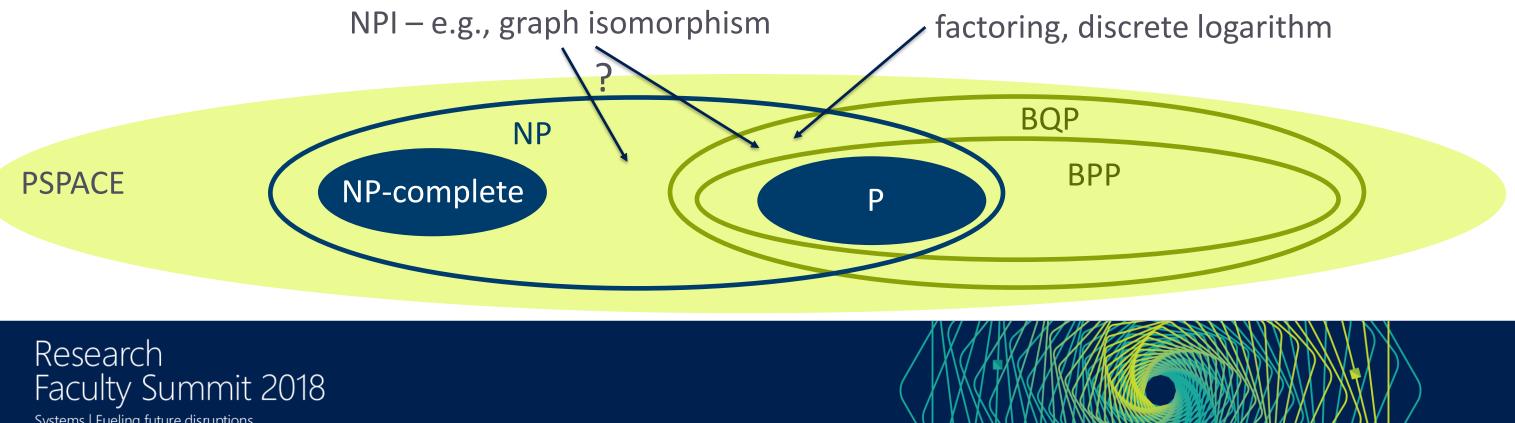




So quantum computers can solve NP-complete problems!?

A problem is in NP if a solution can be verified deterministically in polynomial time.

- Even with quantum computing, it seems that $P \neq NP$ (limited by linearity of operators). Quantum is at least as powerful as classic, thus, we do not know!
- New complexity class: **B**ounded-error **Q**uantum **P**olynomial time (BQP)
 - Quantum version of to Bounded-error Probabilistic Polynomial time (BPP)



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Quantum algorithms are very complex (i.e., weird)

Most quantum programs recombine known algorithmic building blocks!

Amplitude Amplification

Amplify probability of the "right" output

- Using quantum interference
- E.g., Grover's search
- Often $O(\sqrt{2^n})$ iterations



Quantum Walks

Speedup mixing times in randomized algorithms

- Quantum version of random walks
- Between quadratic and (rarely) exponential speedup

Quantum Fourier Transform

DFT on amplitudes of a quantum state

 $O(n \log n)$ gates for 2^n elems Used in factoring and discrete logarithm



operator

Hamiltonian Simulation

Simulate nature 🙂

Exponential speedup (over best known) classical algorithm for quantum effects in physics, chemistry, material science problems



- Quantum teleportation

- . . .

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Phase Estimation

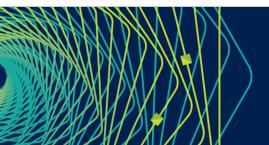
Measure eigenvalues of a unitary

Used to compute eigenvectors Used to solve linear systems Determine eigenvalues in $O\left(\frac{1}{c}\right)$



Others

EPR-pair based proofs/certificates Certified random number generation



How does a quantum computer work?

Qubits are arranged on a (commonly 2D) substrate

Reuse big parts of process technology in microelectronics

Qubits are error prone, need to be highly isolated (major challenge)

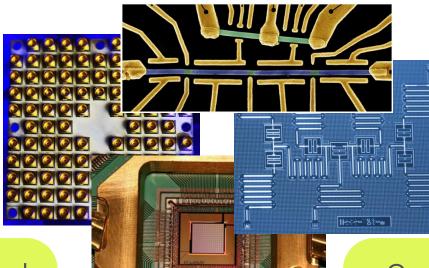
Quantum error correction enabled the dream of quantum computers

> Operations ("gates") are applied to qubits in place!

As opposed to bits flowing through traditional computers!

Quantum systems are most naturally seen as accelerators

Work in close cooperation with a traditional control circuit



Quantum circuits use predication (no control flow)

Circuit view simplifies reasoning but requires classical envelope

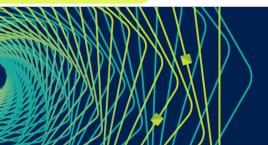
Commonly limited to neighbor interactions between qubits

Operations ("gates") have highly varying complexity

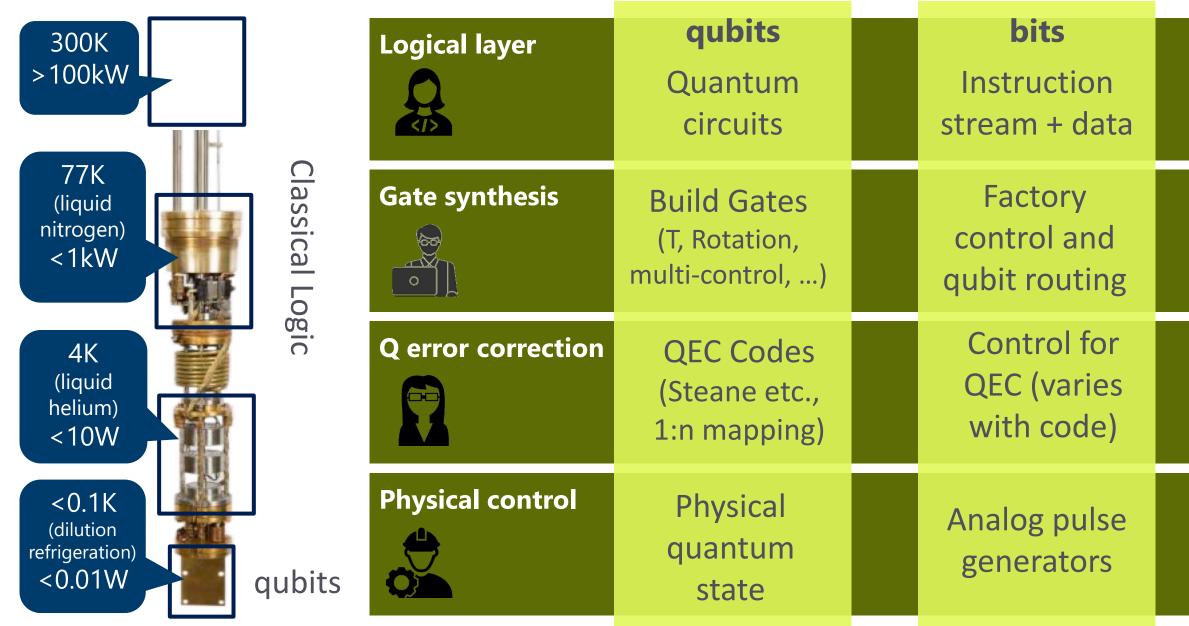
Some are literally free (classical tracking), some are very expensive

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Limited range, may require swapping across chip



Hardware and software architecture for quantum computing



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abstraction Q# programming language

<mark>SW</mark>

MW

MW

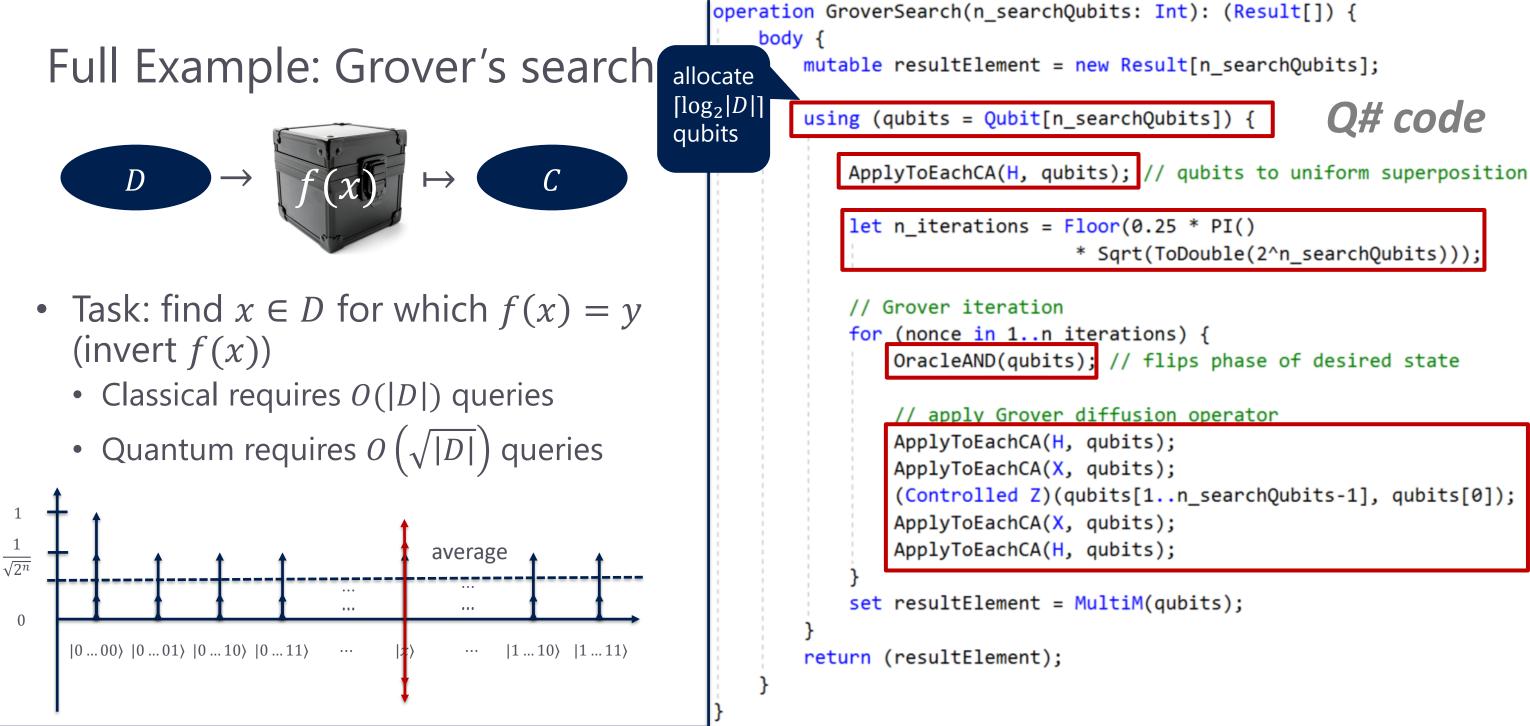
HW

Q intermediate representation

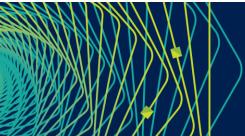
Microcoded instructions

Microcoded instructions

Qubit control pulses



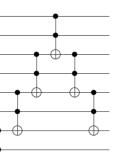
- **Q# code**
- * Sqrt(ToDouble(2^n_searchQubits)));
- (Controlled Z)(qubits[1..n_searchQubits-1], qubits[0]);

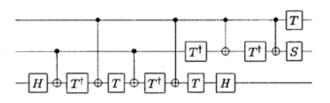


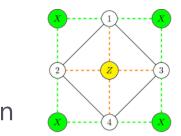
Quadratic speedup? Grover on a real machine

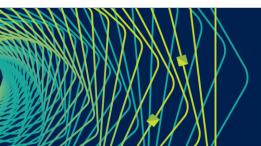
Performance estimates must be understood to be believed (inspired by Donald Knuth's "An algorithm must be seen to be believed")

- 1. Query complexity model how algorithms are developed
 - $T = \left|\frac{\pi}{4}\sqrt{2^n}\right|$ queries ($|D| = 2^n$ represented by *n* bits)
- 2. Express (oracle and diffusion operator) as n-bit unitary
 - Assuming *O* n-bit operations for oracle!
 - $T = O\left|\frac{\pi}{4}\sqrt{2^n}\right|$ n-bit operations $T_t = \left|\frac{\pi}{4}\sqrt{2^n}\right|$
- 3. Decompose unitary into two-bit (+arbitrary rotation) gates
 - $T = O_2 \left| \frac{\pi}{4} \sqrt{2^n} \right| \cdot 2(n-1)$ elementary operations $T_t = \left| \frac{\pi}{4} \sqrt{2^n} \right| \cdot 4(n-1)$
- 4. Design approximate implementations in discrete gate set (using HTHT...)
 - $T = O_{\overline{2}} \left| \frac{\pi}{4} \sqrt{2^n} \right| \cdot 2(n-1)$ discrete T gate operations $T_t = \left| \frac{\pi}{4} \sqrt{2^n} \right| \cdot 48(n-1)$
- 5. Mapping to real hardware (swaps and teleport)
 - Not to simple to model, depends on oracle potentially $\Theta(\sqrt{2^n})$ slowdown
- Quantum error correction
 - Not so simple, depends on quality of physical bits and circuit depth, huge constant slowdown ٠

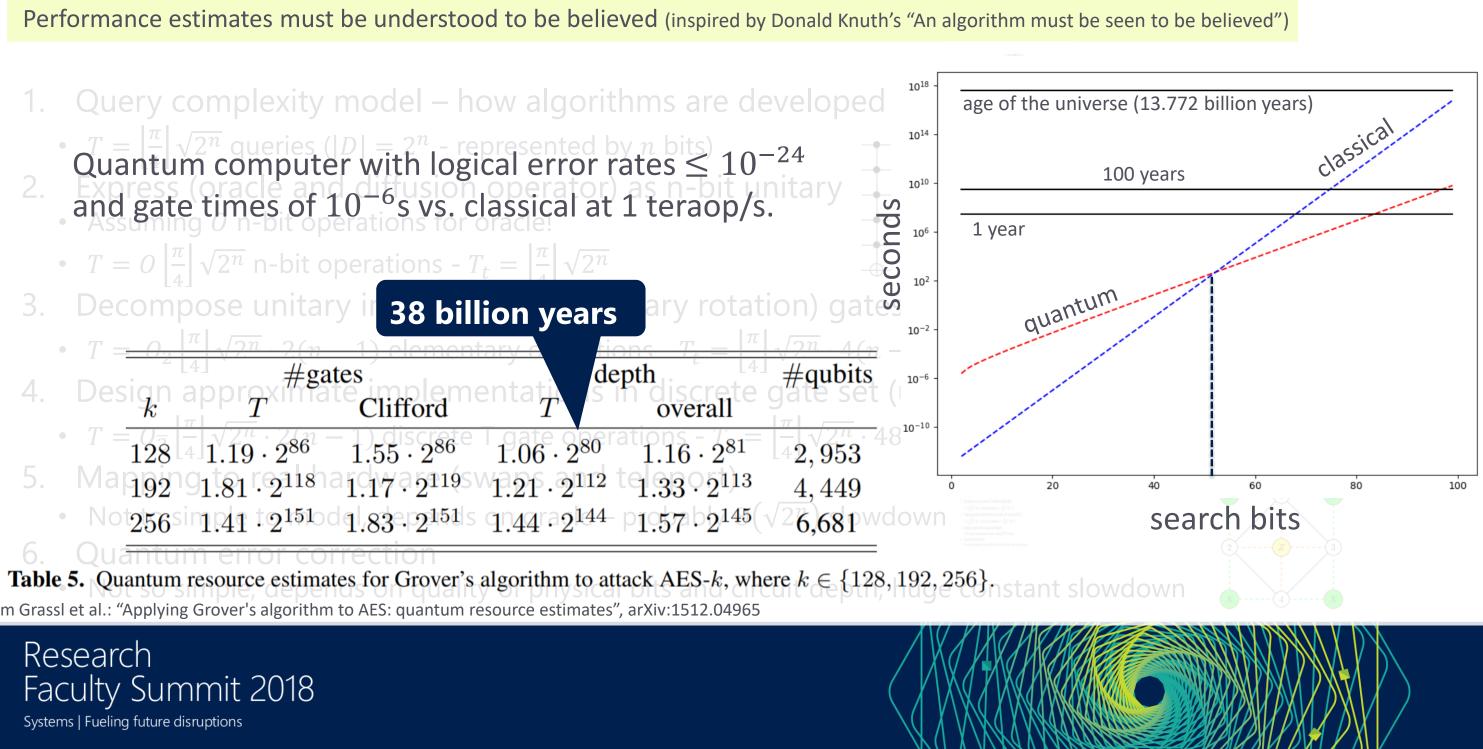








Quadratic speedup? Grover on a real machine



from Grassl et al.: "Applying Grover's algorithm to AES: quantum resource estimates", arXiv:1512.04965

Real applications?

Quantum Chemistry/Physics

- Original idea by Feynman use quantum effects to evaluate quantum effects
- Design catalysts, exotic materials, ...

Breaking encryption & bitcoin

- Big hype destructive impact single-shot (but big) business case
- Not trivial (requires arithmetic) but possible

Accelerating heuristical solvers

- Quadratic speedup can be very powerful!
- Requires much more detailed resource analysis \rightarrow systems problem

Quantum machine learning

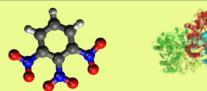
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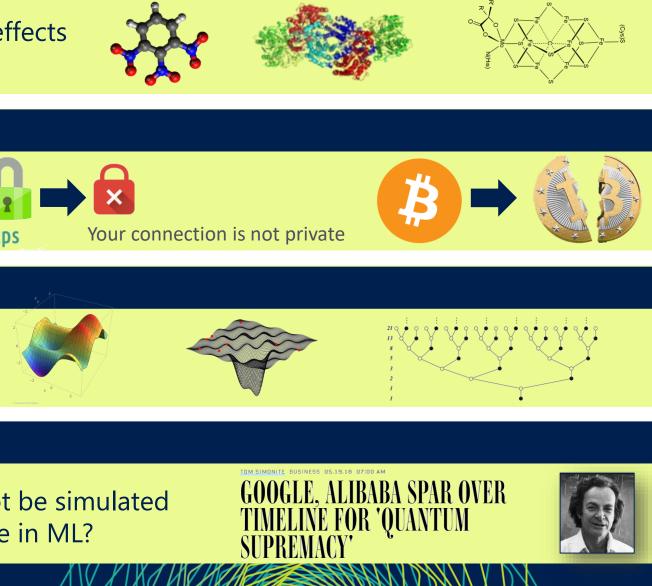
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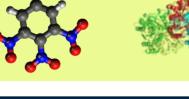
Research

Feynman may argue: "quantum advantage" assumes that circuits cannot be simulated classically \rightarrow they represent very complex functions that could be of use in ML?





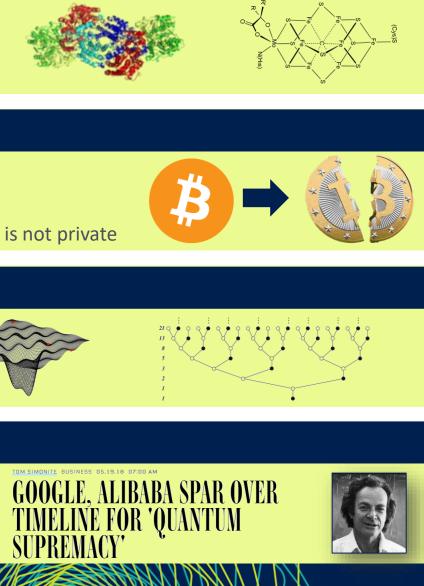














Microsoft Quantum

Thanks!



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- Thanks to: Thomas Haener, Damian Steiger, Martin Roetteler, Nathan Wiebe, Mike Upton, Bettina Heim, Vadym Kliuchnikov, Jeongwan Haah, Dave Wecker, Krysta Svore
- And the whole MSFT Quantum / QuArC team!

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Microsoft Quantum

me on the rocky path to develop my intuition for quantum computation