



NILS BLACH*, Maciej Besta*, Daniele De Sensi, Jens Domke, Hussein Harake, Shigang Li, Patrick Iff, Marek Konieczny, Kartik Lakhotia, Ales Kubicek, Marcek Ferrari, Fabrizio Petrini, Torsten Hoefler

A High-Performance Design, Implementation, Deployment, and Evaluation of The Slim Fly Network

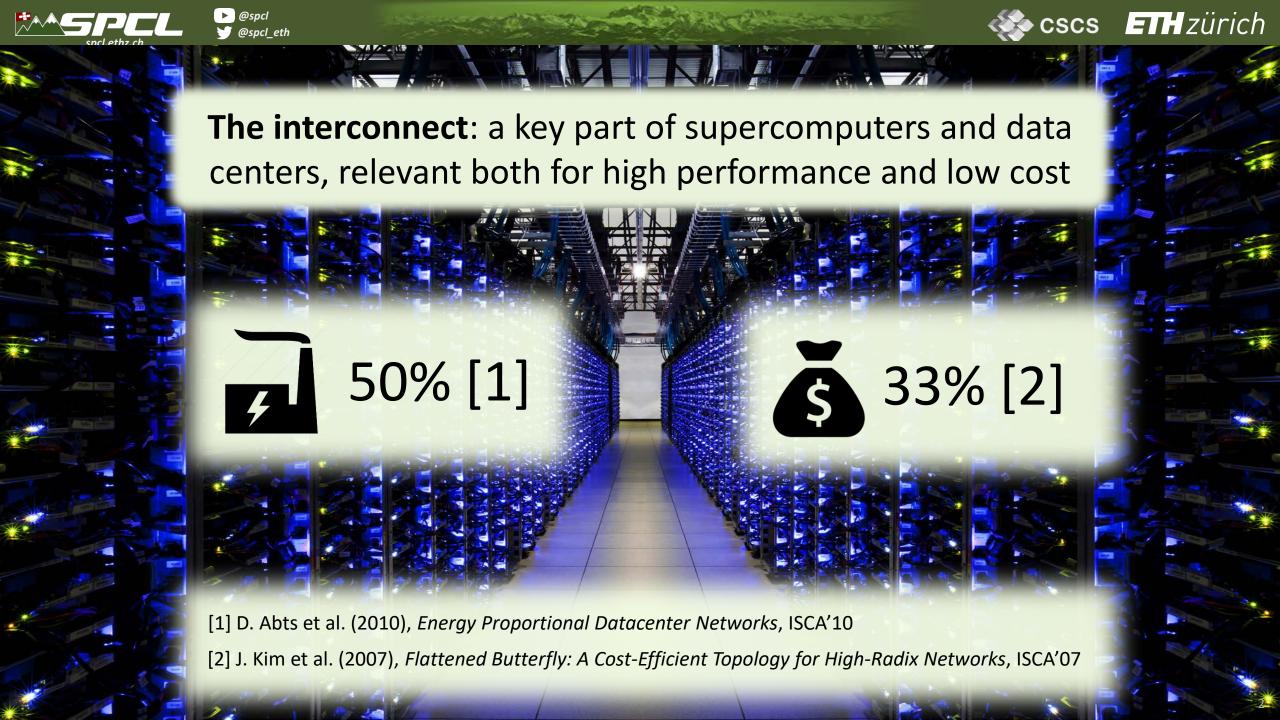
A High-Performance Design, Implementation, Deployment, @ NSDI'24 and Evaluation of The Slim Fly Network

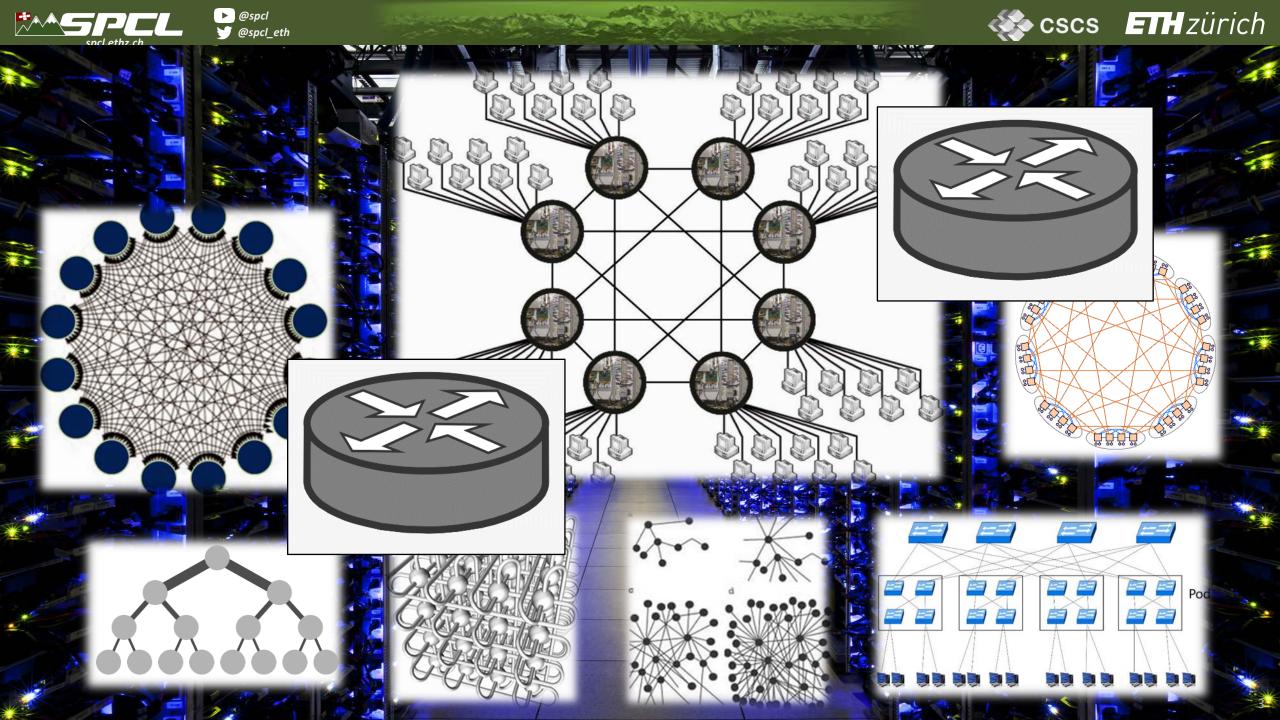
Nils Blach*, Maciej Besta*, Daniele De Sensi*, Jens Domke[†], Hussein Harake[§], Shigang Li*, Patrick Iff*, Marek Konieczny[¶], Kartik Lakhotia[∥], Ales Kubicek*, Marcel Ferrari*, Fabrizio Petrini[∥], Torsten Hoefler*

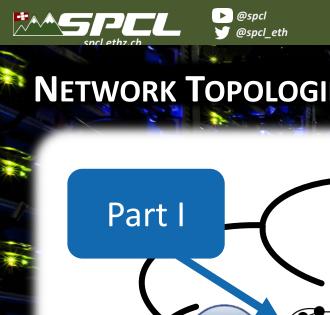


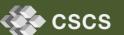
CSCS

Centro Svizzero di Calcolo Scientifico Swiss National Supercomputing Centre



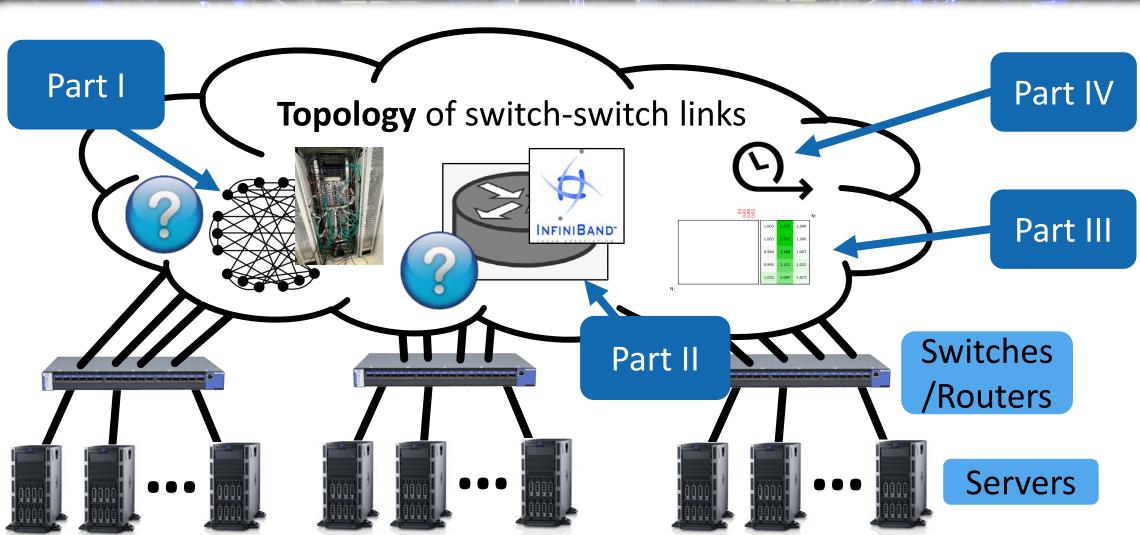
















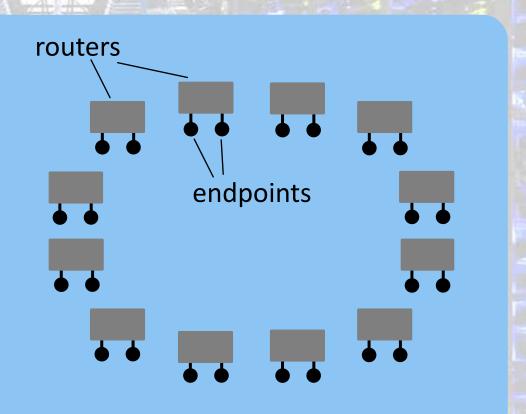


SLIM FLY: AN EFFICIENT LOW-DIAMETER NETWORK TOPOLOGY [1]



Key idea

Lower diameter and thus average path length: fewer cables and routers necessary.







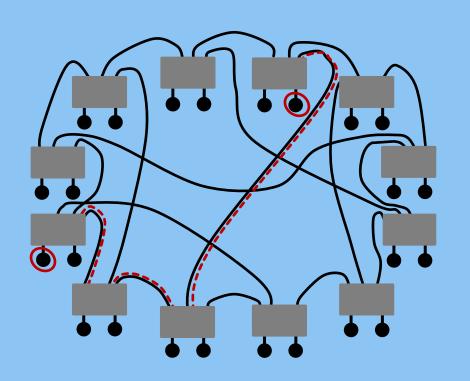


SLIM FLY: AN EFFICIENT LOW-DIAMETER NETWORK TOPOLOGY [1]



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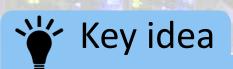






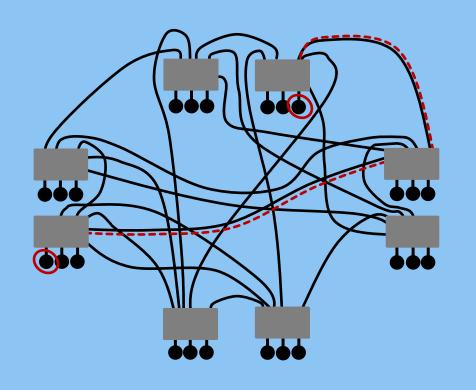


SLIM FLY: AN EFFICIENT LOW-DIAMETER NETWORK TOPOLOGY [1]



Lower diameter \rightarrow more performance, smaller cost, less consumed power

Lower diameter and thus average path length: fewer cables and routers necessary.







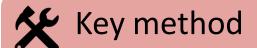


SLIM FLY: AN EFFICIENT LOW-DIAMETER NETWORK TOPOLOGY

Fix diameter (e.g., D = 2)

Fix radix k (router port count) as needed

With Moore Bound optimization, the network gets as many routers as possible (cost per router is minimized)

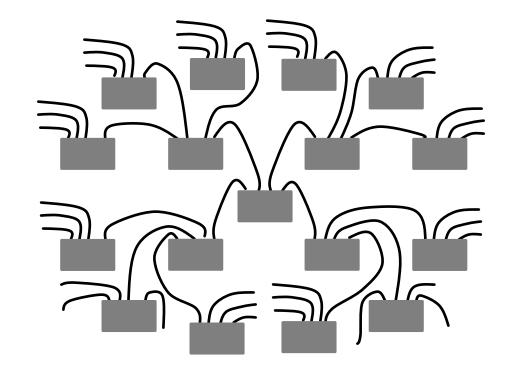


Optimize towards the Moore Bound [1]:

the upper bound on the *number of vertices* in a graph with given *diameter D* and *radix k*.

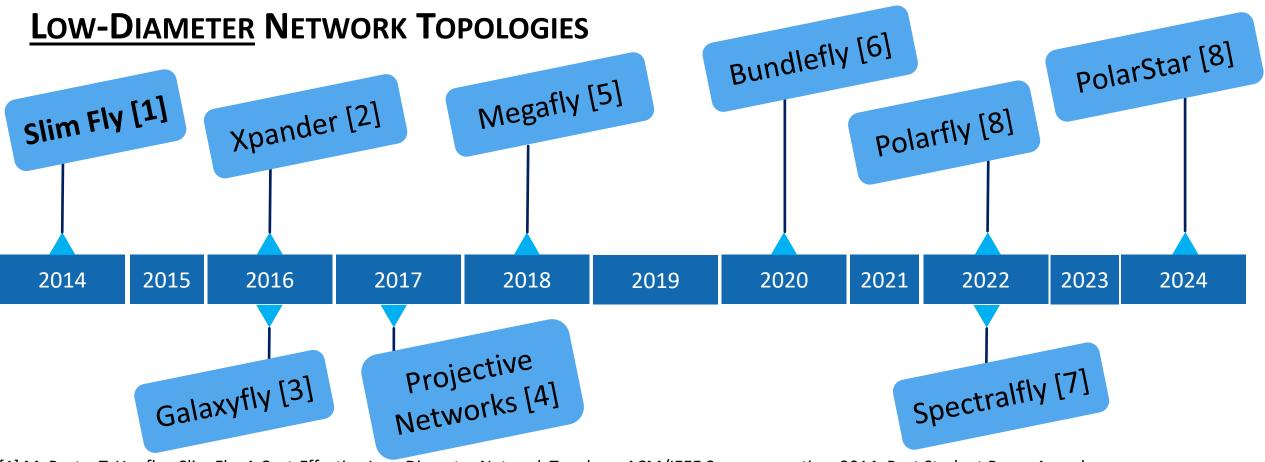
$$MB(D,k) = 1 + k + k(k-1) + k(k-1)^{2} + \cdots$$

$$= 1 + k \sum_{i=0}^{D-1} (k-1)^{i}$$









- [1] M. Besta, T. Hoefler. Slim Fly: A Cost-Effective Low-Diameter Network Topology. ACM/IEEE Supercomputing, 2014. Best Student Paper Award
- [2] A. Valadarsky et al. Xpander: Towards optimal-performance datacenters. ACM CoNEXT, 2016
- [3] Fei Lei et al. Galaxyfly: A novel family of flexible-radix low-diameter topologies for large-scales interconnection networks. ACM/IEEE Supercomputing, 2016
- [4] Cristóbal Camarero et al. Projective Networks: Topologies for Large Parallel Computer Systems. ACM/IEEE TPDS, 2017
- [5] M. Flajslik et al. Megafly: A topology for exascale systems. ICHPC 2018
- [6] F. Lei et al. Bundlefly: a low-diameter topology for multicore fiber. ACM/IEEE Supercomputing, 2020
- [7] S. Aksoy et al. Spectralfly: Ramanujan graphs as flexible and efficient interconnection networks. arXiv preprint, 2022
- [8] K. Lakhotia et al. PolarFly: A Cost-Effective and Flexible LowDiameter Topology. ACM/IEEE Supercomputing, 2022
- [9] K. Lakhotia et al. PolarStar: Expanding the Scalability Horizon of Diameter-3 Networks. ACM SPAA 2024





These networks look complicated...

Moore graph

Article Tall

From Wikipedia, the free encyclopedia

In graph theory, a **Moore graph** is a regular graph whose girth (the shortest cycle length) is more than twice its diameter (the distance between the farthest two vertices). If the degree of such a graph is d and its diameter is k, its girth must equal 2k+1. This is true, for a graph of degree d and diameter k, if and only if its number of vertices equals

$$1+d\sum_{i=0}^{k-1}(d-1)^i,$$

a) Step 1: Constructing Base Ring \mathbb{Z}_q : Let $\mathbb{Z}_q = \{0,1,...,q-1\}$ be a commutative ring with modulo addition and multiplication. We have to find a primitive element ξ of \mathbb{Z}_q . ξ is an element of \mathbb{Z}_q that generates \mathbb{Z}_q : all non-zero elements of \mathbb{Z}_q can be written as ξ^i $(i \in \mathbb{N})$. In general, there exists no universal scheme for finding ξ [45], however an exhaustive search is viable for smaller rings; all the SF MMS networks that we tested were constructed using this approach.

2020 | 2021 | 2022 | 2023 | 202

b) Step 2: Constructing Generator Sets X and X': In the next step we utilize ξ to construct two sets X and X' called generators [35]. For $\delta=1$ we have $X=\{1,\xi^2,...,\xi^{q-3}\}$ and $X'=\{\xi,\xi^3,...,\xi^{q-2}\}$ (consult [35] for other formulae). We will use both X and X' while connecting routers.

Are they really so complex?

Can we route/deploy them?

ter S

Let's see an example Slim Fly

[7] S. Aksoy et al. Spectrality: Ramanujan graphs as flexible and efficient

[8] K. Lakhotia et al. PolarFly: A Cost-Effective and Flexible LowDiameter Topology. ACM/IB

[9] K. Lakhotia et al. PolarStar: Expanding the Scalability Horizon of Diameter-3 Networks. ACM SPAA 2024



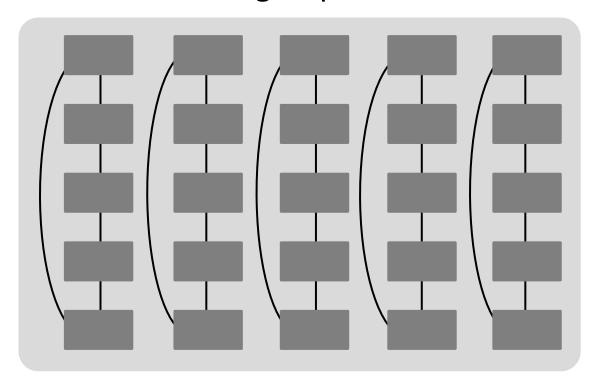




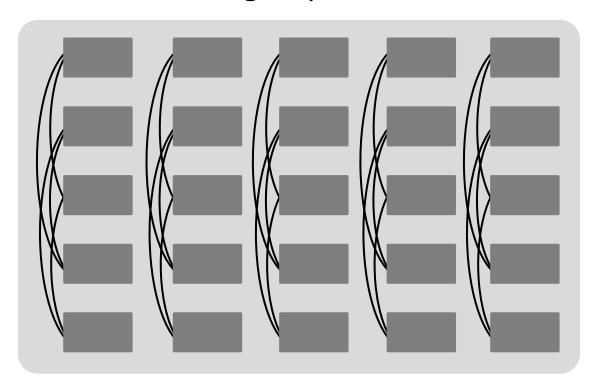
DEPLOYING SLIM FLY: STRUCTURE INTUITION

50 routers, 200 servers (omitted)

A subgraph with identical groups of routers



A subgraph with identical groups of routers



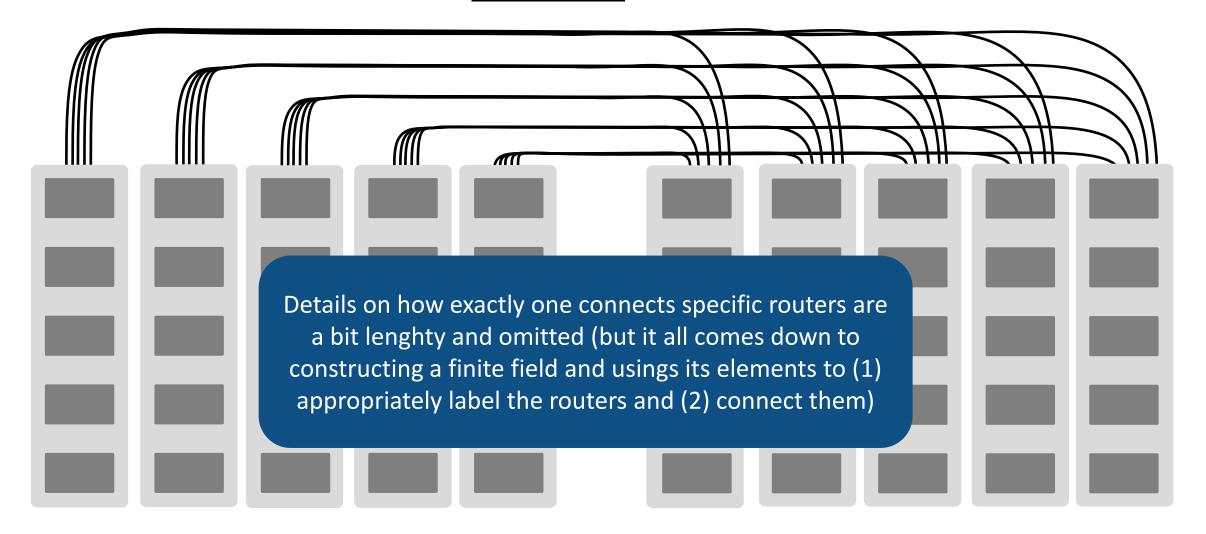






DEPLOYING SLIM FLY: STRUCTURE INTUITION

50 routers, 200 servers (omitted)



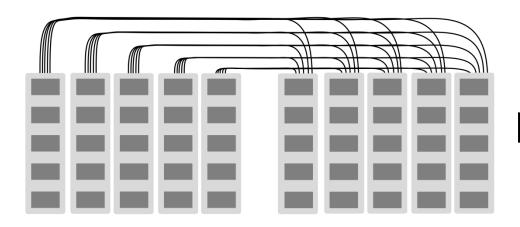
Groups form a fully-connected bipartite graph

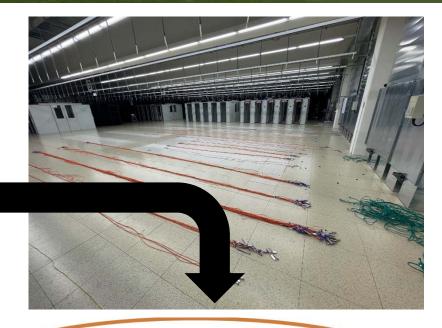






The First Slim Fly Construction







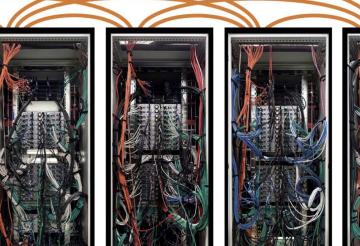
Orange IB cables: Optical cables for inter-rack

5 x IB Switches

Login Node

5 x IB Switches

InfiniBand connections. Each bunch contains 10 links

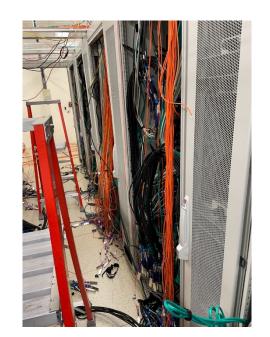


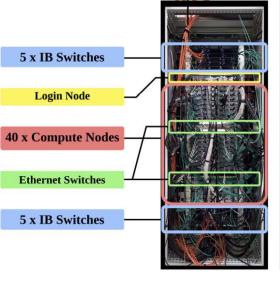
Black IB cables: Copper cables for intra-rack

InfiniBand connections

Colored Ethernet cables:

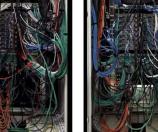
- The blue, white and green cables are Ethernet cables











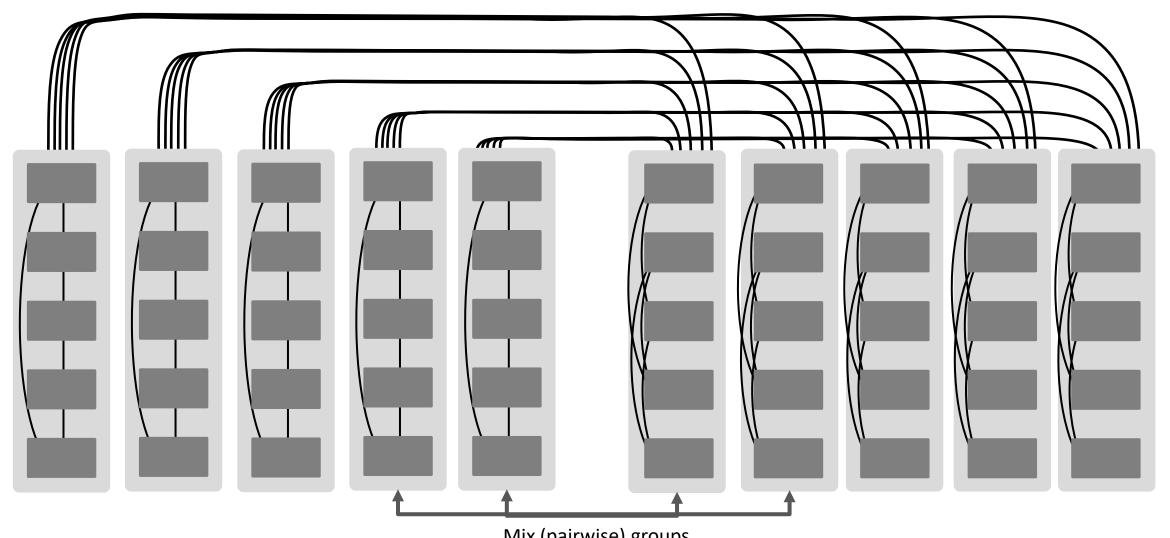








50 routers, 200 servers (omitted)



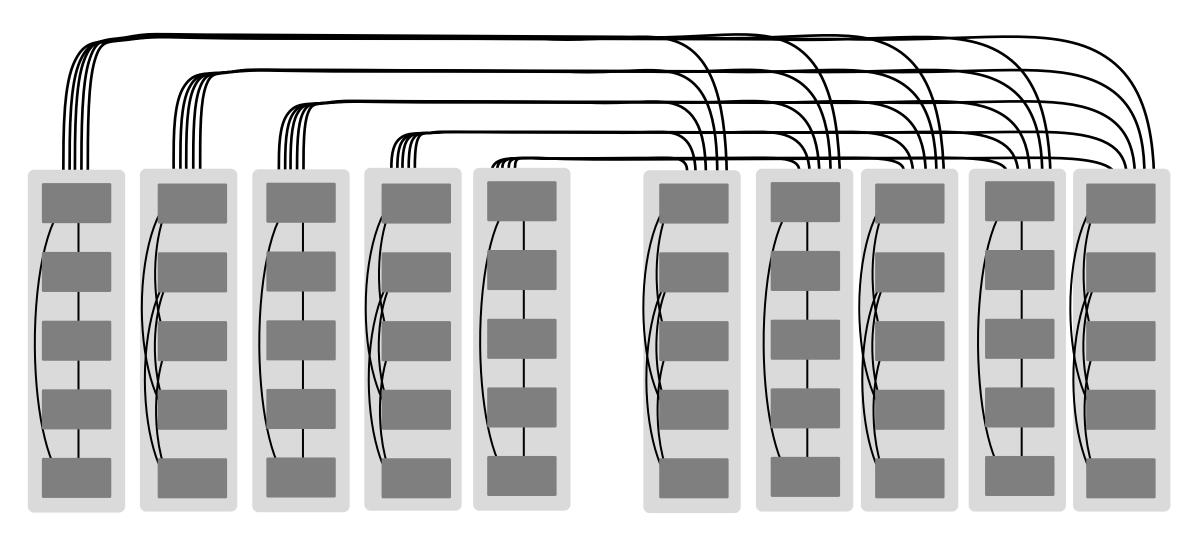
Mix (pairwise) groups with different cabling patterns to shorten inter-group cables







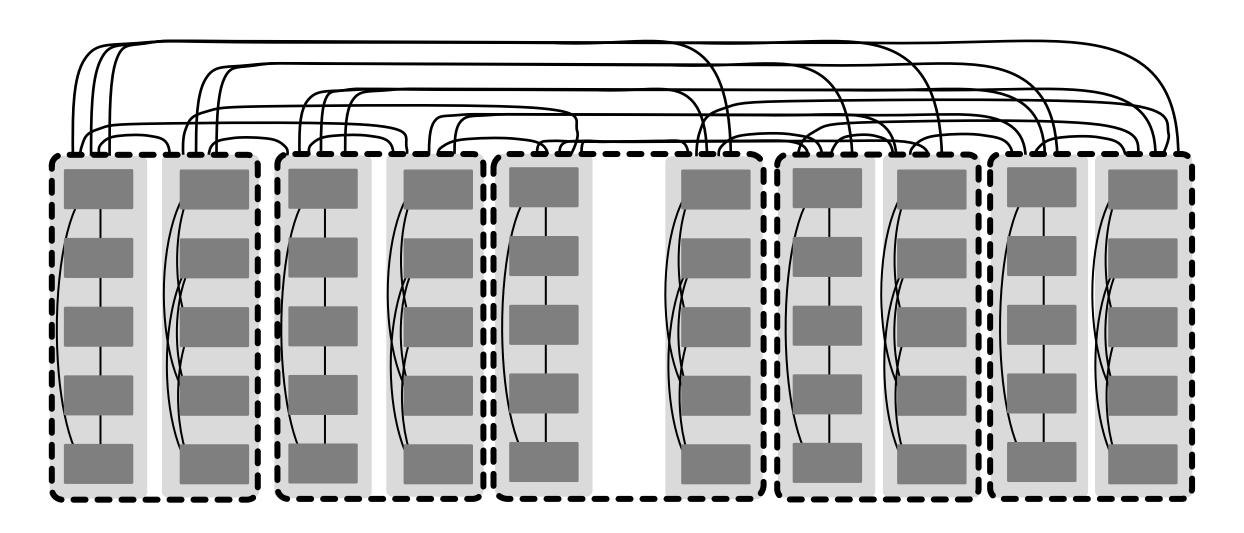
50 routers, 200 servers (omitted)







50 routers, 200 servers (omitted)

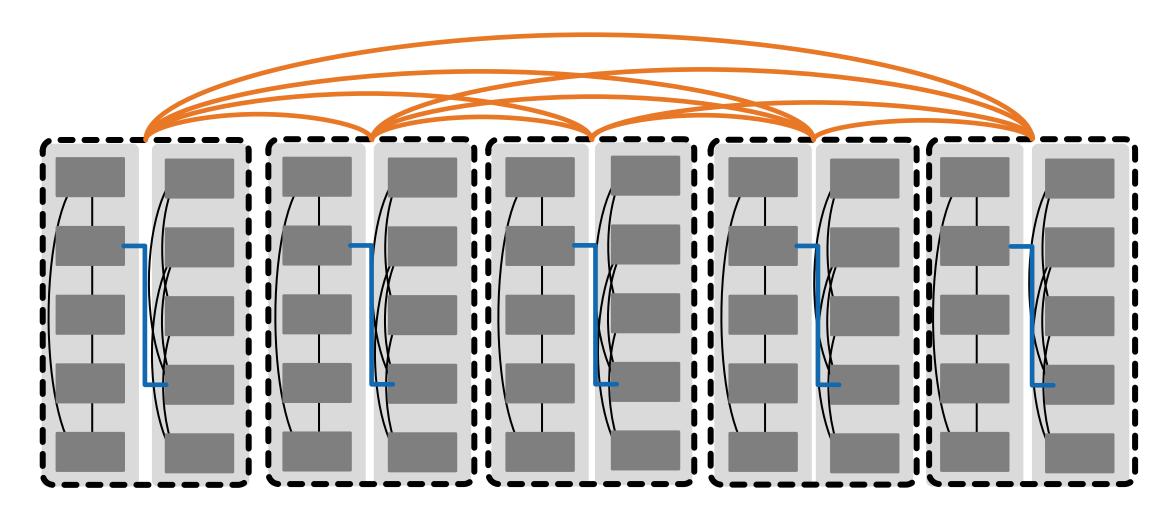








50 routers, 200 servers (omitted)



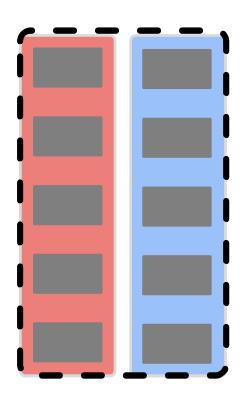
Racks form a fully-connected graph

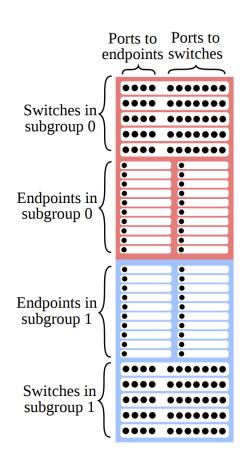


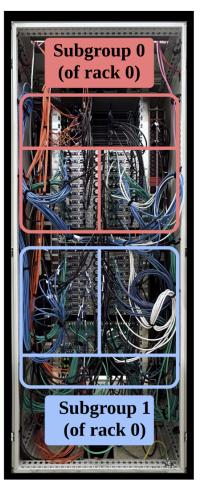














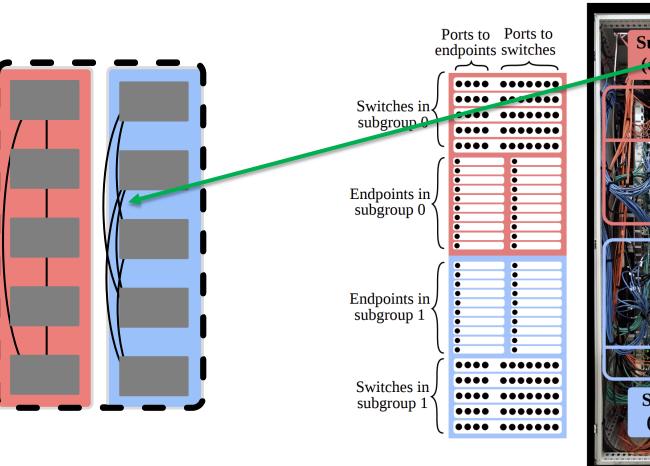


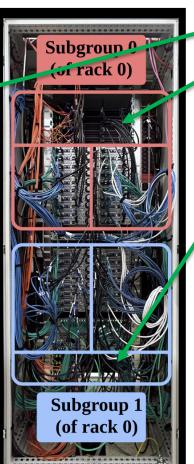




Step 1

DEPLOYING SLIM FLY – STEP 1: INTRA-SUBGROUP CONNECTIONS







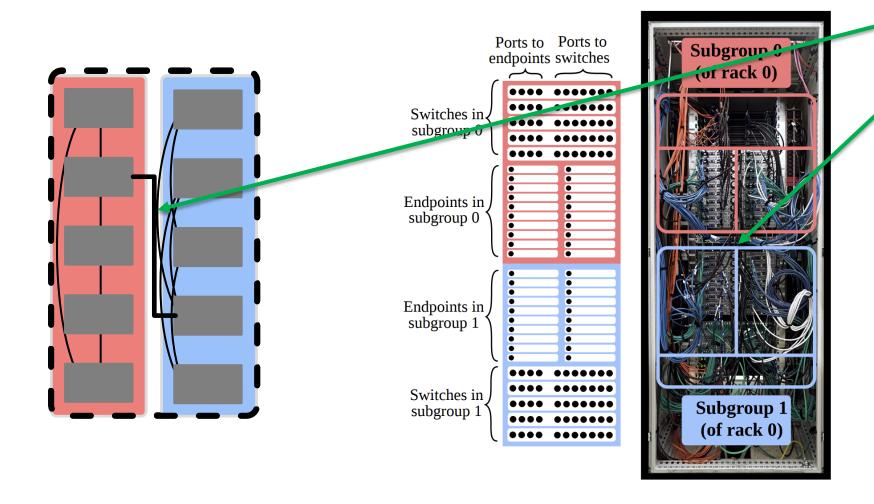






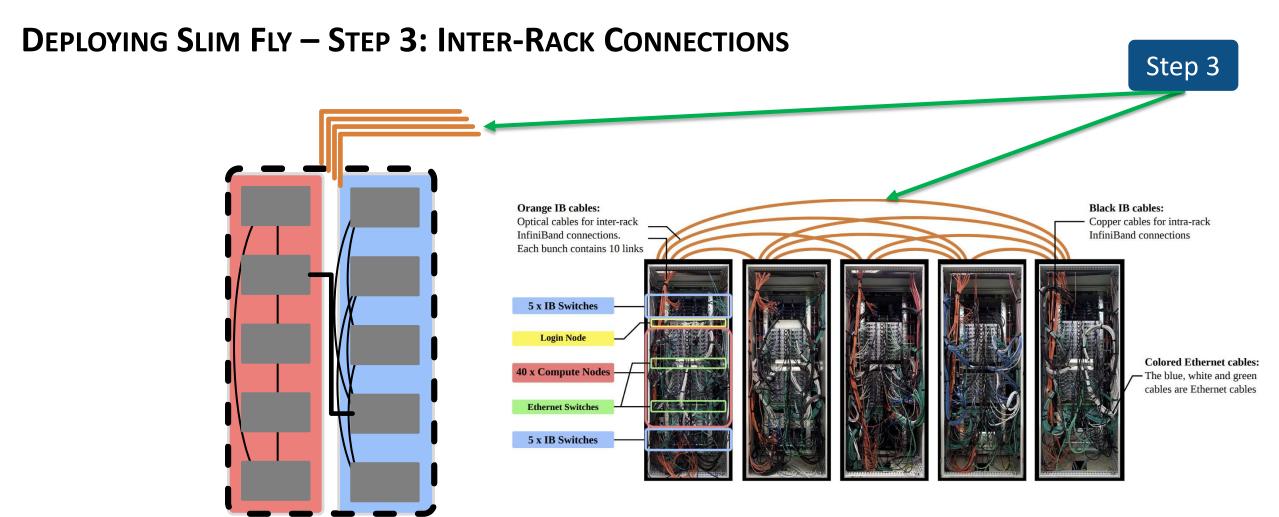
DEPLOYING SLIM FLY – STEP 2: INTER-SUBGROUP CONNECTIONS

Step 2







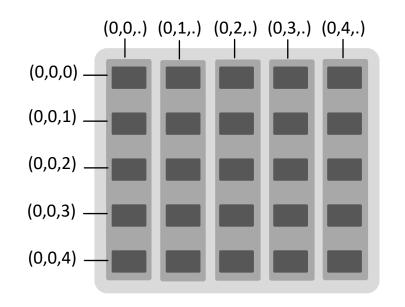


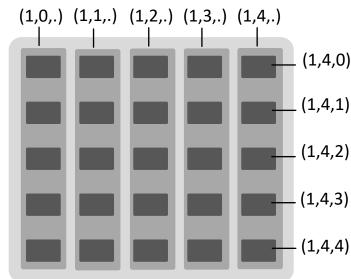






DEPLOYING SLIM FLY – VERIFICATION





Connectivity determined by the following algebraic equations

router (0, x, y) is connected to (0, x, y') iff $y - y' \in X$; router (1, m, c) is connected to (1, m, c') iff $c - c' \in X'$; router (0, x, y) is connected to (1, m, c) iff y = mx + c;

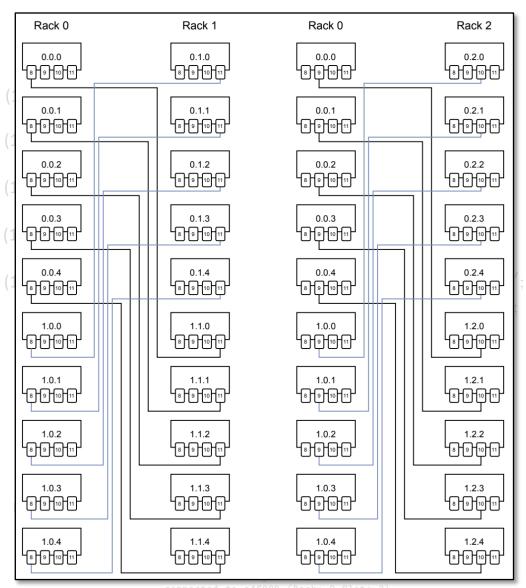






DEPLOYING SLIM FLY - VERIFICATION

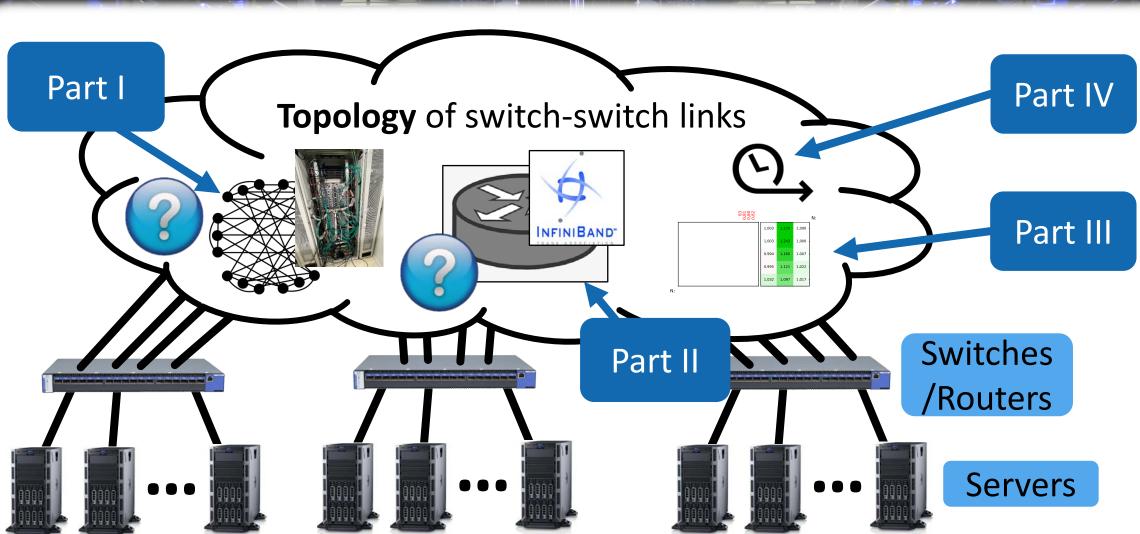








NETWORK TOPOLOGIES: SETTING & PRESENTATION PLAN





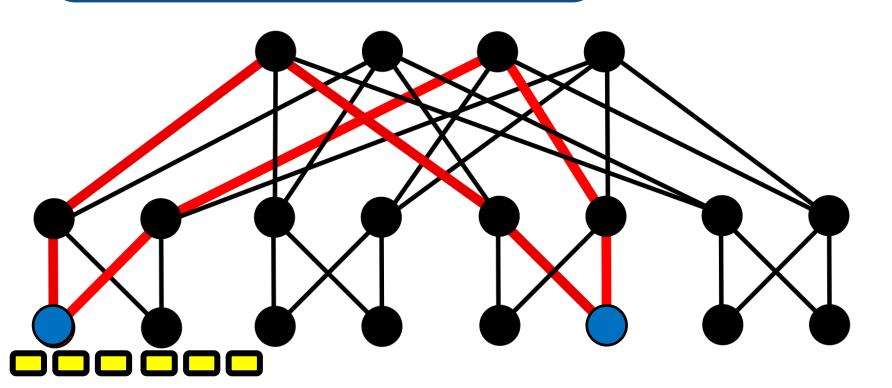






ROUTING IN FAT TREES

High-performance routing is facilitated by **numerous multiple** shortest paths of equal lengths between any endpoints









ROUTING IN FAT TREES



High-performance routing is facilitated by <u>numerous multiple</u>
shortest paths of equal lengths
between any endpoints

Network Working Group Request for Comments: 2992

Category: Informational

ECMP

INFORMATIONAL

C. Hopps NextHop Technologies November 2000

Analysis of an Equal-Cost Multi-Path Algorithm

Established techniques for using multipathing & plethora of designs available

-- الاقتا -- الاقتا -- الاقتا -- الاقتا -- الاقتا -- الاقتا التقا التقا

Source routing for flowible DC fabric [117]

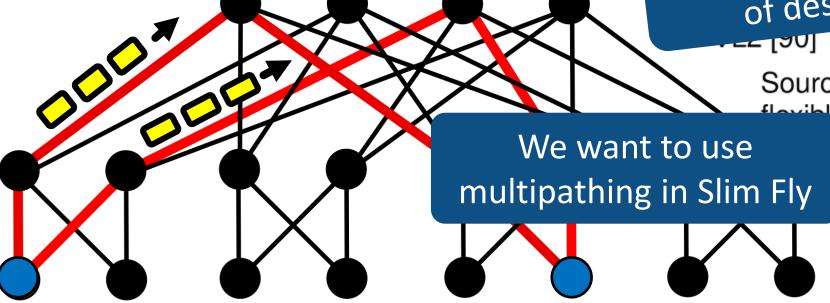
Monsoon [91]

PortLand [160] SPAIN [158]

ECMP-VLB [123]

Work by Linden et al. [215]

Work by Suchara et al. [204]





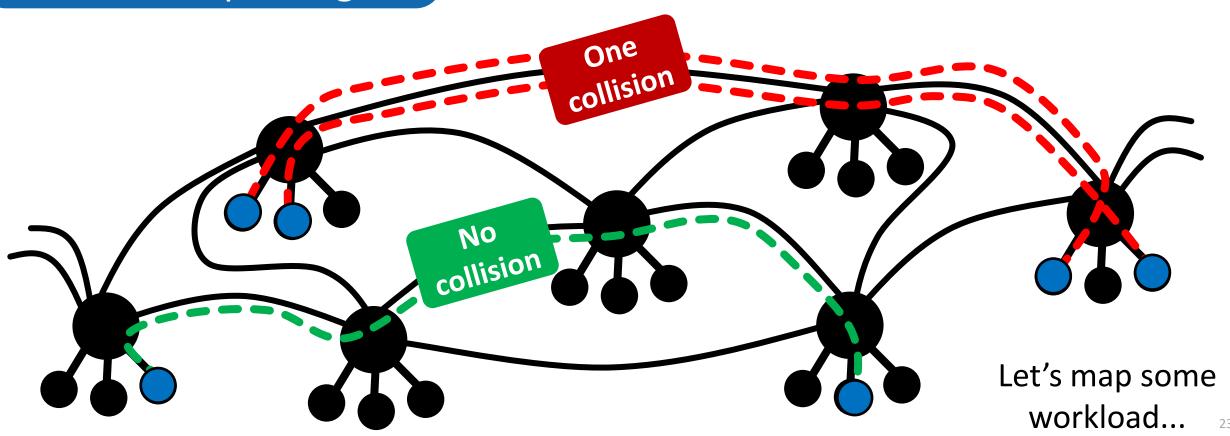








Flows collide!



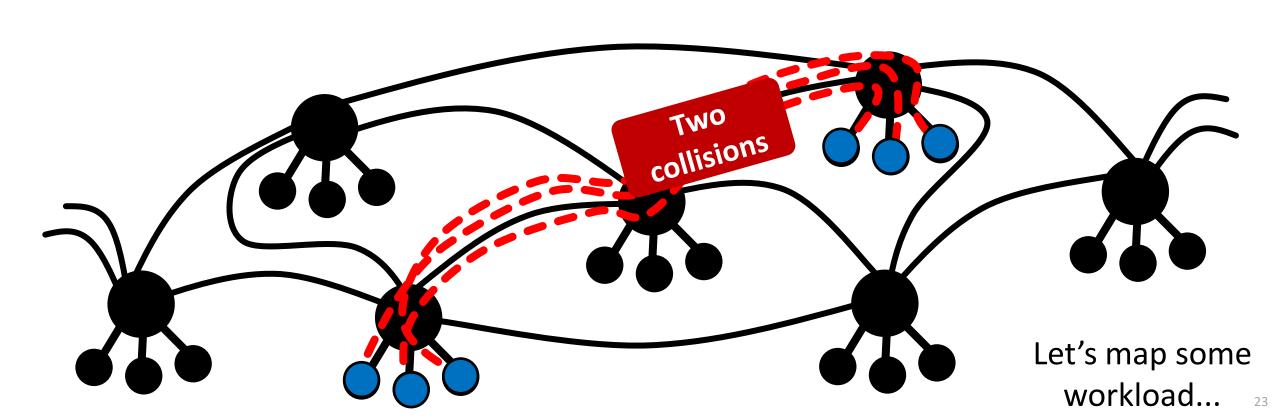












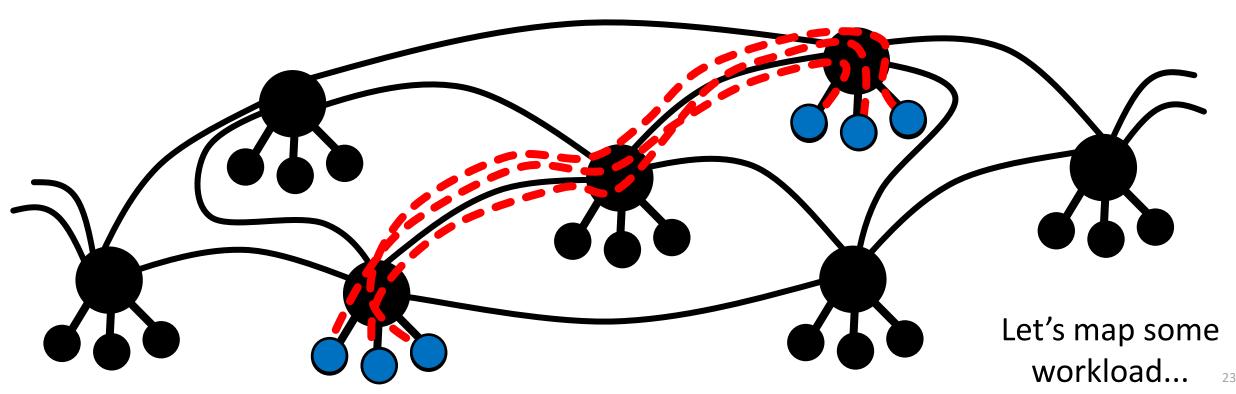








Flows collide!





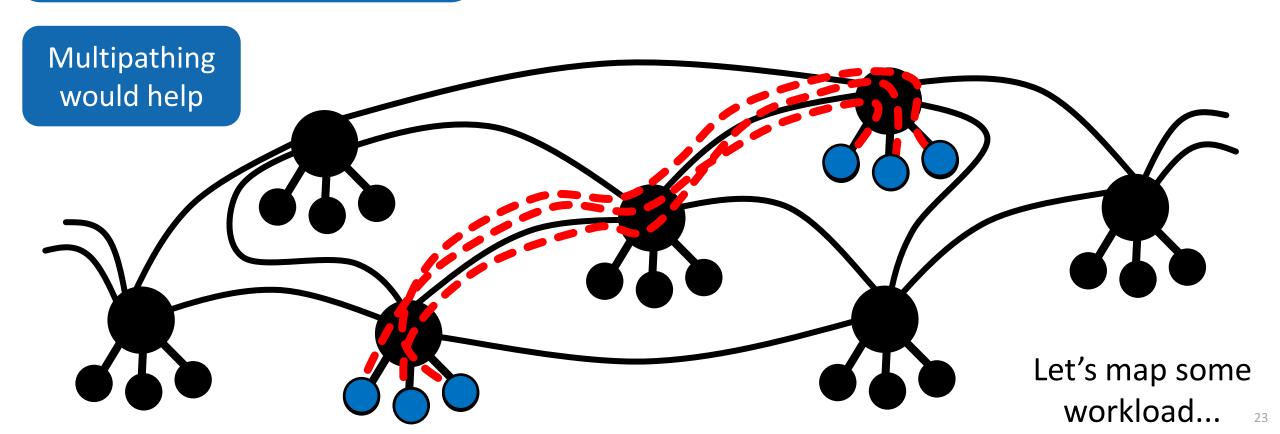














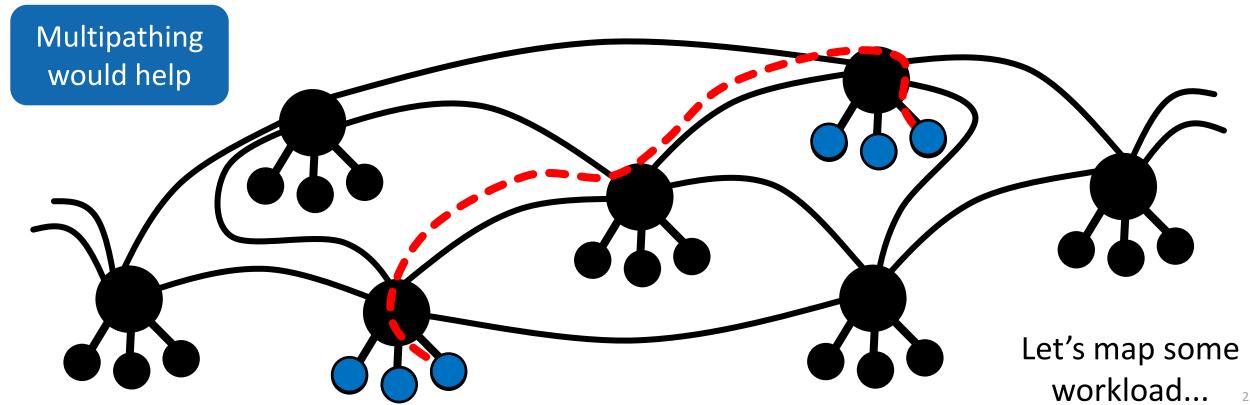














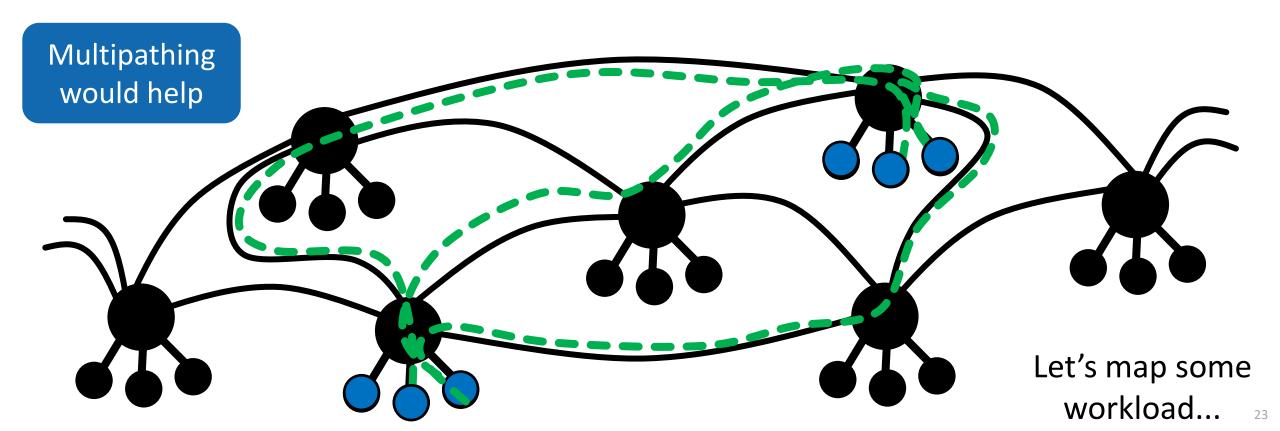






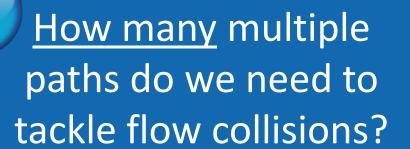












Are there enough multiple paths in Slim Fly?

Key Insight 1: We need three disjoint paths per router pair to handle [almost all] colliding flows [1]

Key Insight 2: In most cases, there is only enough path diversity when considering "almost" minimal paths [1]



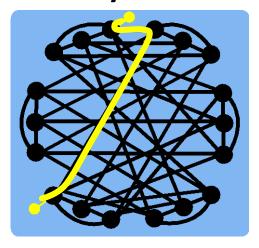


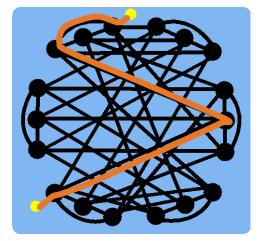


NOVEL LAYERED ROUTING PROTOCOL

Layer 0:

Layer 1:

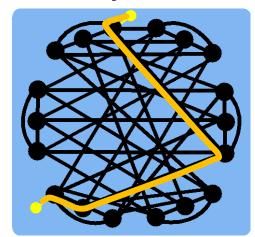




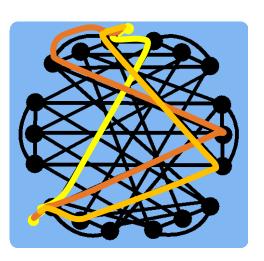
Layer 2:

Layer 0: minimal paths

Layers 1-...: non-minimal paths



Key idea: distribute & encode different paths across "routing layers"



We minimize the overlap of paths between layers







NOVEL LAYERED ROUTING PROTOCOL

Layer 0:

Layer 1:



Key idea: distribute & encode different paths across "routing layers"

Layer 0: minimal paths

What are example problems that we need to tackle when implementing this with IB?

Layers 1-...: non-minimal paths



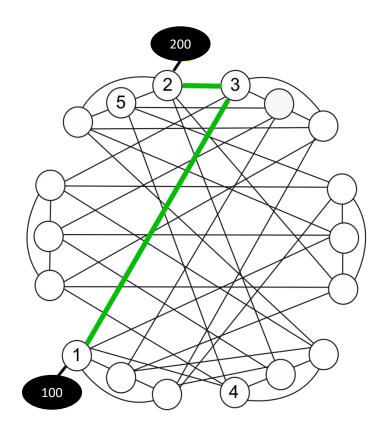
We minimize the overlap of paths between layers







InfiniBand - Addressing



Key idea: use multiple LIDs
(LID = Local Identifier) for
the same endpoint to
encode multiple paths

Problem 1: How do we introduce layers in InfiniBand?

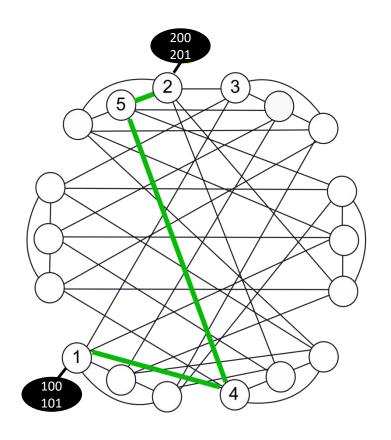
Switch 1	
Destination LID	Next Hop
200	3







InfiniBand - Addressing



Key idea: use multiple LIDs
(LID = Local Identifier) for
the same endpoint to
encode multiple paths

Problem 1: How do we introduce layers in InfiniBand?

Switch 1					
Destination LID	Next Hop				
200	3				
201	4				







IB Address Space Limitations

40 Ports

#Layers	Max #Switches	Max #Endnodes	#Endnodes per Switch	Network radix
1	578	7514	13	25
2	587	7514	13	25
4	578	7514	13	25
8	450	5400	12	23
16	288	2592	9	18
32	162	1134	7	13
64	98	588	6	11
128	72	360	5	9

Problem 2: How many layers can we support?

IB supports at most 49'151 unicast addresses

For a given number of layers, what is the largest Slimfly network that IB can support, while maintaining full global bandwidth?



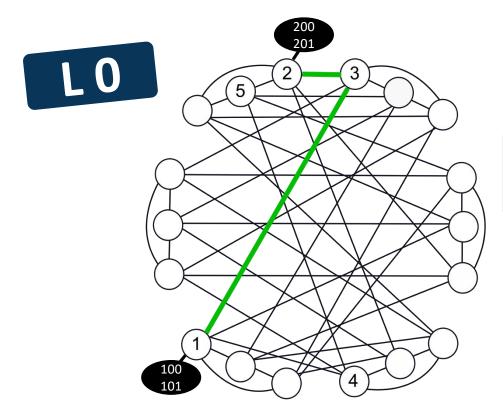




InfiniBand - Layer Generation Algorithm

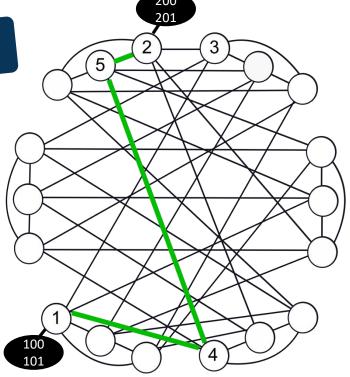
For each switch pair find and add an almost-minimal path in every layer (use minimal paths in Layer 0)

Problem 3: Given that we want 3 disjoint paths, how many layers do we need?





Switch 1				
Destination LID	Next Hop			
200	3			
201	4			

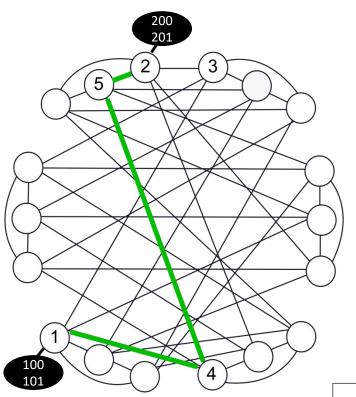








InfiniBand - Layer Generation Algorithm



All packets that are in switch 5 that want to reach switch 2 have to take the direct link in this layer (due to IB's destination based routing)

Problem 4: Can we fail to add an almost-minimal disjoint path?

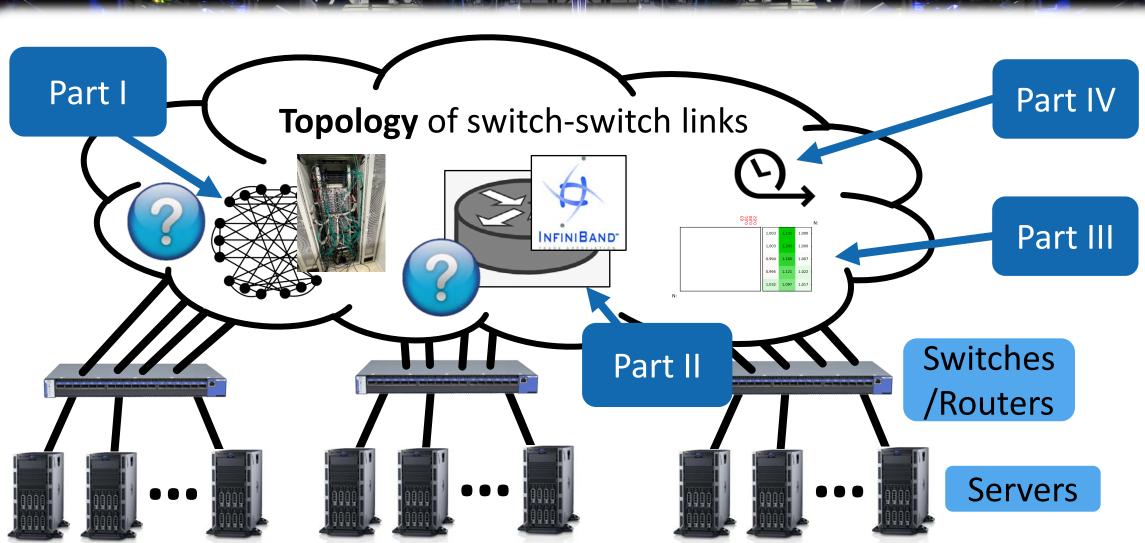
Setting: We are trying to add a non-minimal path to this layer for the switch pair (5, 2), after a path for the pair (1, 2) has been inserted

Switch 5					
Destination LID	Next Hop				
201	2				





NETWORK TOPOLOGIES: SETTING & PRESENTATION PLAN



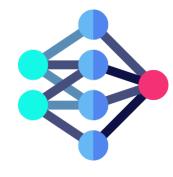








Evaluation











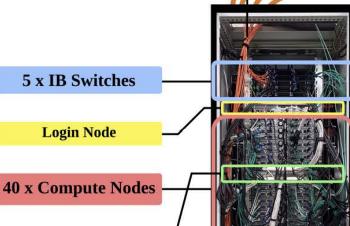
Orange IB cables:

5 x IB Switches

Login Node

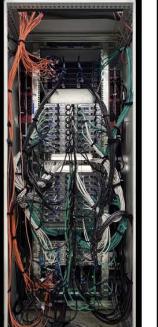
Optical cables for inter-rack InfiniBand connections.

Each bunch contains 10 links

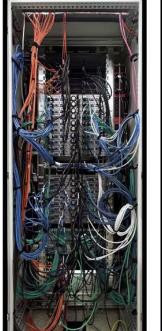




Ethernet Switches









Black IB cables:

Copper cables for intra-rack InfiniBand connections

Colored Ethernet cables:

The blue, white and green cables are Ethernet cables







Comparison Baselines & Setup

Theoretical analysis

$$-\sum_{v \in V} \sum_{l=1,\dots,n} f_{is_i vl} \cdot \delta_{v,\sigma_l(s_i,t_i)} + T(s_i,t_i) \cdot \mathcal{T} \le 0, \quad i = 1, 2, \dots, k$$
(5)

$$\sum_{i=1,\dots,k} \sum_{l=1,\dots,n} f_{iuvl} \cdot \delta_{v,\sigma_l(u,t_i)} \le c(u,v), \quad \forall (u,v) \in E$$

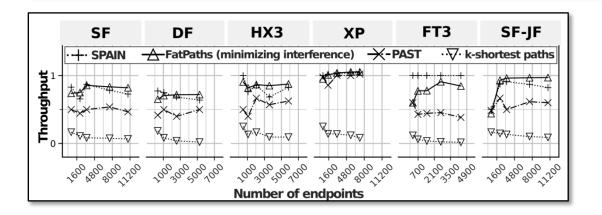
$$(6)$$

$$\sum_{v \in V} f_{iuvl} \cdot \delta_{v,\sigma_l(u,t_i)} - \sum_{v \in V} f_{ivul} \cdot \delta_{u,\sigma_l(v,t_i)} = 0, \quad i = 1,\dots,k, \quad l = 1,\dots,n, \forall u \in V \setminus \{s_i,t_i\}$$

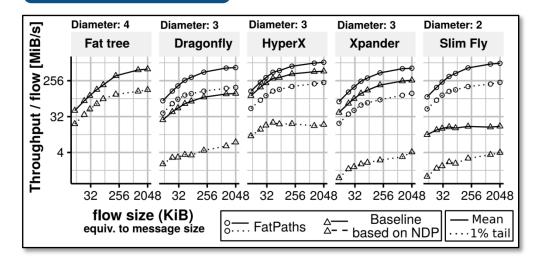
$$(7)$$

$$\sum_{v \in V} \sum_{l=1,\dots,n} f_{is_ivl} \cdot \delta_{v,\sigma_l(s_i,t_i)} \le \mathcal{T}_{upperbound} \cdot T(s_i,t_i), \quad i = 1,\dots,k$$
(8)

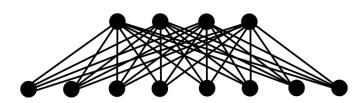
$$\sum_{v \in V} \sum_{l=1,\dots,n} f_{ivs_i l} \cdot \delta_{s_i,\sigma_l(v,t_i)} = 0, \quad i = 1,\dots,k$$
(9)

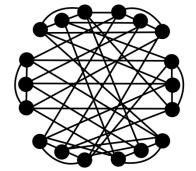


Simulations



Real testbed comparisons



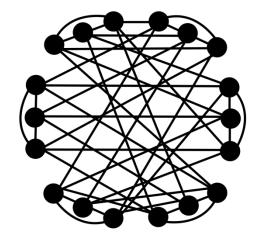


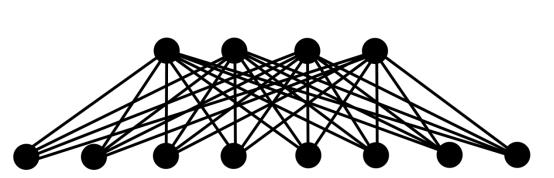






Comparison Baselines & Setup





<u>Baseline:</u> 2-Level Non-Blocking Fat-Tree constructed using the same hardware

Rank Placement Strategy: Linear for both Slim Fly (SF) and Fat-Tree (FT)

Routing

Networks

Baseline: Deadlock-Free SSSP (DFSSSP) [1] routing, a standard IB protocol

[1] J. Domke et al. Deadlock-Free Oblivious Routing for Arbitrary Topologies. IPDPS, 2011.





Microbenchmarks

In most scenarios, SF is comparable to FT

For 8 and 16-node configurations – especially with smaller message sizes – the FT displays marginal advantages.

Reason: FT has 16 nodes per switch (SF: 4), leading to more localized, zero inter-switch hop traffic

MPI Bcast - SF vs. FT

1.01	1.00	0.97	0.96	1.00	0.52	1.01	1.00
1.01	1.00	0.96	0.97	1.00	1.05	1.07	0.95
1.03	1.00	0.98	0.94	1.01	0.98	1.21	1.24
1.02	1.00	0.99	0.84	1.02	0.95	0.81	1.32
1.02	1.01	0.81	0.97	1.07	0.87	0.88	0.94
1.02	1.01	0.82	1.01	1.00	1.05	0.90	0.97
1.03	1.02	0.81	1.02	1.01	0.95	1.07	0.98
1.02	1.00	0.87	1.16	0.95	0.95	0.95	1.00
1.02	1.01	1.00	1.00	0.99	0.96	0.90	1.41
1.04	1.03	0.97	1.00	1.09	1.01	1.03	1.09
1.03	1.00	0.99	0.94	0.99	0.96	0.95	0.99
1.05	1.06	1.03	0.95	0.96	1.02	0.97	1.00
1.01	1.01	0.98	0.93	1.01	1.00	1.01	1.00
1.00	1.01	1.00	0.92	0.97	1.00	0.98	0.99
0.98	1.01	0.98	0.90	0.97	0.97	1.37	1.00
1.03	1.01	0.95	0.91	0.97	1.01	0.99	1.02
1.01	1.03	0.96	0.90	0.96	1.01	0.97	1.03
1.06	1.02	0.96	0.89	0.96	1.01	0.98	1.06
1.02	1.00	0.99	0.89	0.97	1.03	0.98	1.03
0.97	1.03	0.94	0.85	0.96	1.00	1.02	1.07
1.01	1.02	0.94	0.89	0.96	1.03	1.01	1.02
1.00	1.02	0.98	0.89	0.98	1.02	1.02	1.06
1.00	1.04	0.96	0.87	0.97	1.00	1.00	1.06
0.99	1.05	0.95	0.86	1.00	1.03	0.98	1.05
0.98	1.02	0.93	0.85	0.98	1.04	1.02	1.02
1.00	0.98	0.96	0.86	0.98	1.03	1.01	1.02

N:

MPI Allreduce - SF vs. FT

1.05	1.11	1.07	1.05	1.03	0.67	0.71	2.95
1.03	1.14	1.10	1.09	1.07	0.71	0.79	2.64
0.89	1.05	1.02	1.02	1.08	0.72	0.78	2.73
0.90	1.02	1.03	1.01	1.06	0.82	0.87	3.10
1.01	1.12	1.02	1 02	1.06	0.90	0.97	0.95
1.00	1.02	1.01	0.90	1.07	0.97	1.06	0.98
1.01	0.98	1.02	0.94	1.02	1.08	1.07	1.04
1.04	1.01	1.01	0.91	1.01	1.02	1.04	1.00
1.01	1.01	0.95	1.00	1.00	1.00	0.98	0.99
1.00	1.01	0.99	0.98	1.00	0.97	0.98	1.08
1.03	1.01	1.01	1.01	0.98	0.96	0.98	0.99
0.99	1.00	0.98	1.00	1.00	0.97	0.97	0.97
1.01	1.05	0.93	0.84	0.84	0.89	0.86	1.29
1.09	1.06	0.95	0.95	0.93	0.97	0.98	1.00
0.95	1.01	0.99	0.94	0.97	1.02	1.03	1.00
0.95	1.03	0.97	0.93	1.06	1.04	1.01	1.01
0.93	1.01	0.99	0.93	1.05	0.98	1.05	1.01
0.94	0.87	0.97	0.90	1.03	1.01	1.02	1.07
1.19	1.12	1.09	0.89	1.02	1.07	1.00	1.02
1.08	1.01	1.06	0.94	1.00	1.03	1.02	1.04
1.11	0.99	1.01	0.90	0.99	1.02	1.02	1.00
1.34	0.95	1.02	0.99	0.94	0.98	1.03	1.02
1.28	1.02	0.92	0.93	0.97	1.10	1.04	1.01
1.07	1.10	0.91	0.89	1.02	1.04	0.97	1.02

N:

odes







Microbenchmarks

Traffic congestion on the (often) single shortest path between a few switches.

HW's lack of adaptive load balancing support (which we do enable in the protocols) limits its practical improvement

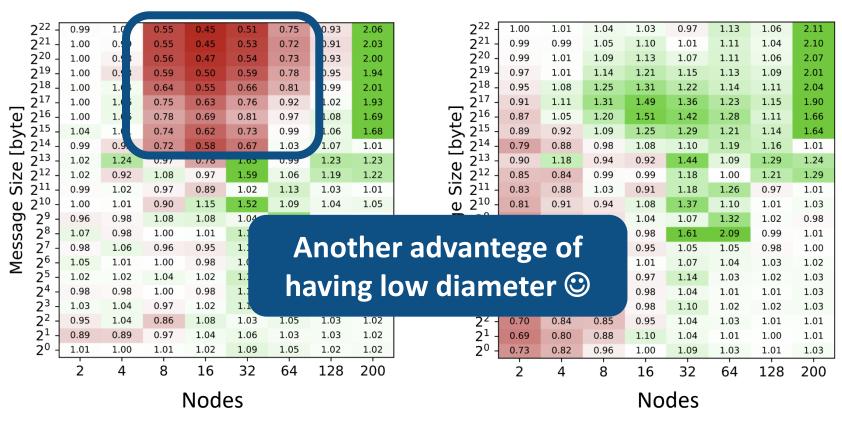
Random placement for SF, overcomes this bottleneck

Linear placement in SF

MPI Alltoall - SF vs. FT

Random placement in SF

MPI Alltoall – SF vs. FT

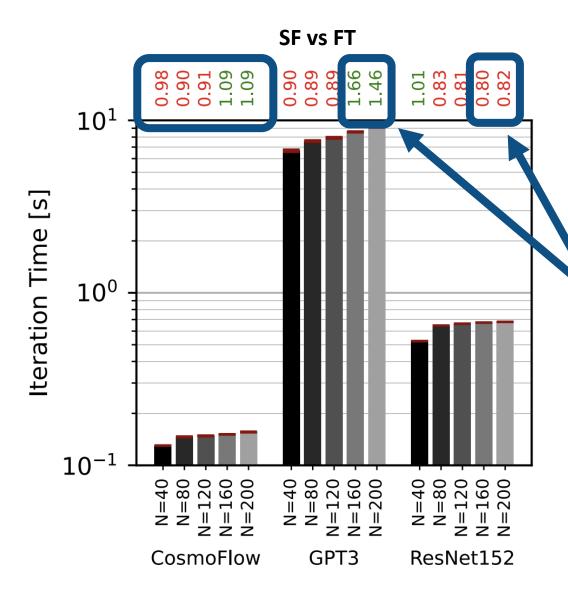








Deep Learning Proxy Workloads



CosmoFlow: Data + operator parallelism, requires allgather, reduce-scatter, allreduce, and point-to-point

ResNet152: Pure data parallelism, only requires allreduce

GPT-3: Data + operator + pipeline parallelism, requires allreduce and point-to-point

Both GPT-3 and ResNet152 predominantly rely on allreduces at higher node counts...

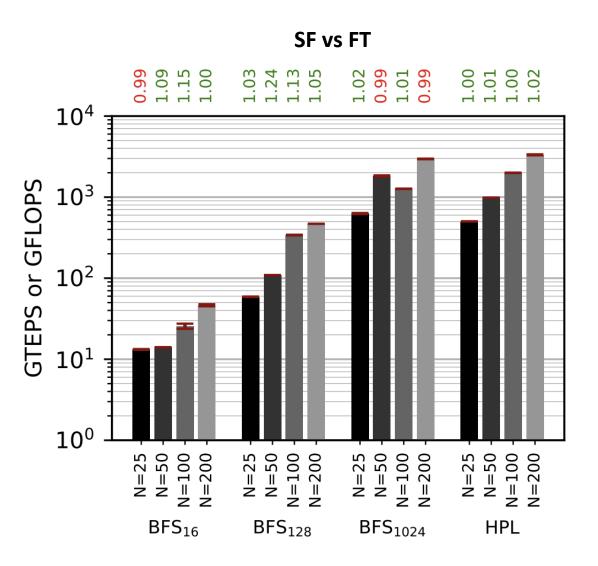
...but GPT-3 handles significantly larger messages than ResNet152. Expectedly, the performance trend of GPT-3 matches the trend of MPI Allreduce for the high node count configurations







HPC Benchmarks



SF competes effectively with FT in terms of performance

SF is effective for scaling HPC benchmarks







Routing Improvements

Layered Routing vs DFSSSP

Routing Improvement



CosmoFlow GPT3 ResNet152

Layered Routing outperforms
DFSSSP

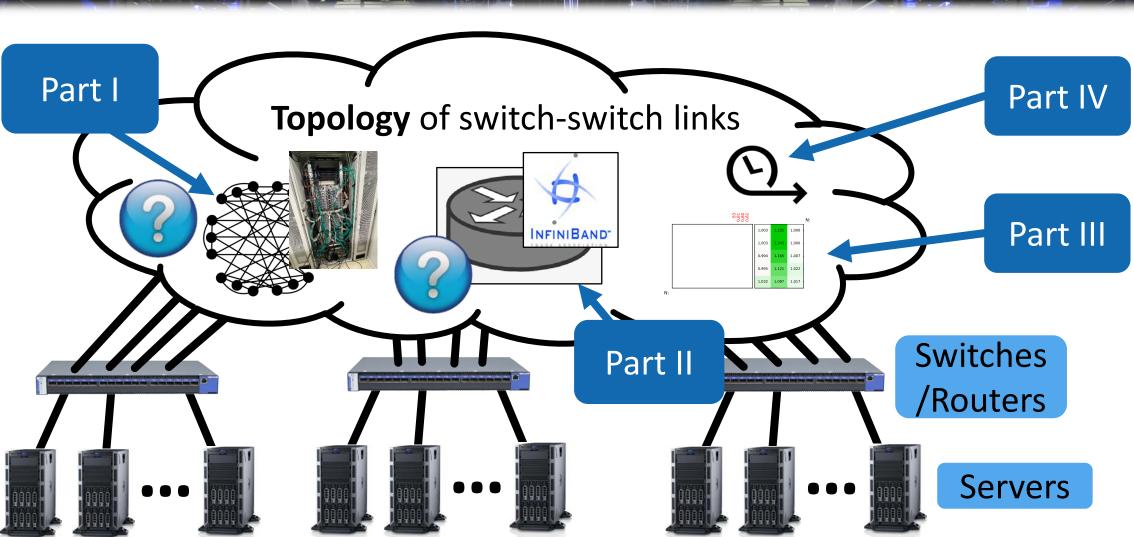
This is thanks to the multipathing support (despite not being able to leverage adaptivity)

















Cluster Use Cases, Research Outcomes, & Future Potential

Swing: Short-cutting Rings for Higher Bandwidth Allreduce

Daniele De Sensi Sapienza University of Rome Tommaso Bonato ETH Zurich David Saam RWTH Aachen University

Torsten Hoefler ETH Zurich **Past**

...

HammingMesh: A Network Topology for Large-Scale Deep Learning

Torsten Hoefler*†, Tommaso Bonato*, Daniele De Sensi*, Salvatore Di Girolamo*, Shigang Li*, Marco Heddes†, Jon Belk†, Deepak Goel†, Miguel Castro†, and Steve Scott†

Congestion Benchmarking and Visualization of Large-Scale Interconnection Networks

@ SC'22,
Reproducibility
Advancement Award,
Invited as CACM
Research Highlight

@ NSDI'24

A High-Performance Design, Implementation, Deployment, and Evaluation of The Slim Fly Network

Nils Blach*, Maciej Besta*, Daniele De Sensi*, Jens Domke[†], Hussein Harake[§], Shigang Li*, Patrick Iff*, Marek Konieczny[¶], Kartik Lakhotia[∥], Ales Kubicek*, Marcel Ferrari*, Fabrizio Petrini[∥], Torsten Hoefler*

Present/Future

Foundations of performance measures for interconnects

Testing SOTA interconnects (HammingMesh, PolarFly, PolarStar)

Enabling cheap computations by filling idleness gaps on HPC systems ("HPC for Free").

Testing new batch scheduler policies, new paradigms, etc.

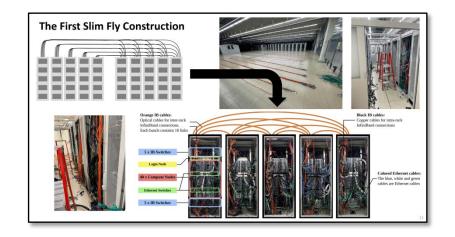
...

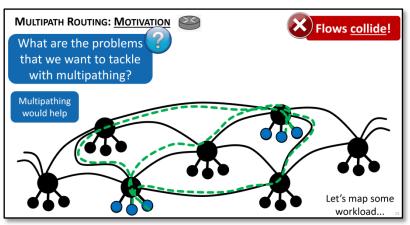
Bandwidth-Optimal, Fully-Offloaded Collectives

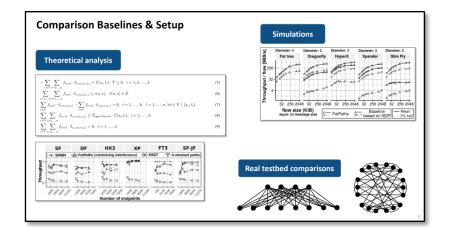


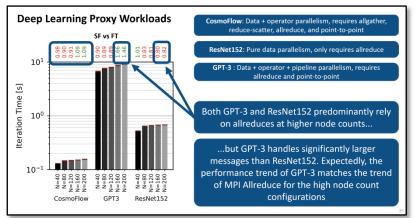


Conclusions









More of SPCL's research:



... or spcl.ethz.ch

