Design of Parallel and High-Performance Computing

Fall 2017

Lecture: Lock-Free and distributed memory

Motivational video: https://www.youtube.com/watch?v=PuCx50FdSic

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ETH

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

Administrivia

- Final project presentation: Monday 12/18 (two weeks)
 - Should have (pretty much) final results
 - Show us how great your project is
 - Some more ideas what to talk about:

Which architecture(s) did you test on?

How did you verify correctness of the parallelization?

Use bounds models for comparisons [1]!

(Somewhat) realistic use-cases and input sets?

Emphasize on the key concepts (may relate to theory of lecture)!

What are remaining issues/limitations?

- Report will be due in January!
 - Still, starting to write early is very helpful --- write rewrite rewrite (no joke!)
 - Maybe last unit today: Entertainment with bogus results!

[1]: T. Hoefler, R. Belli: Scientific Benchmarking of Parallel Computing Systems, IEEE/ACM SC15

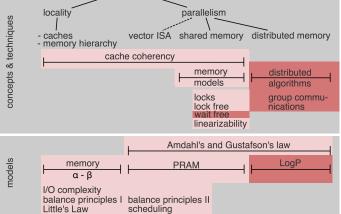
Review of last lecture

- Various multi-process locks
 - Bakery
 - Spinning locks

Contention issues etc.

- Queue-based locks
 - CLH. MCS
- MCS do not forget @
 - Queue-based only wait for predecessor
 - Local spinning (good for non-CC NUMA)
 - Unlock not trivial (cleans up races in lock)
- Scientific benchmarking!
 - Follow the rules, but remember they're not exhaustive!
 - Think before measuring

DPHPC Overview



Goals of this lecture

- Practical lock properties
 - RW locks
 - Lock properties/issues (deadlock, priority inversion, blocking vs. spinning)
 - Competitive spinning
- Locked and lock-free tricks
 - Fine-grained locking
 - RW locking
 - Optimistic synchronization
 - Lazv locking
 - Lock-free (& wait-free)
- Maybe: finish wait-free/lock-free
 - Consensus hierarchy
 - The promised proof!

More Practical Optimizations

- Let's step back to "data race"
 - (recap) two operations A and B on the same memory cause a data race if one of them is a write ("conflicting access") and neither $A\rightarrow B$ nor $B\rightarrow A$
 - So we put conflicting accesses into a CR and lock it! Remember: this also guarantees memory consistency in C++/Java!
- Let's say you implement a web-based encyclopedia
 - Consider the "average two accesses" do they conflict?



Number of edits (2007-11/27/2017): 921,644,695 Average views per day: ~200,000,000

→ 0.12% write rate

Reader-Writer Locks

- Allows multiple concurrent reads
 - Multiple reader locks concurrently in CR
 - Guarantees mutual exclusion between writer and writer locks and reader and writer locks
- Syntax:
 - read_(un)lock()
 - write_(un)lock()

A Simple RW Lock

- Seems efficient!?
 - Is it? What's wrong?
 - Polling CAS!
- Is it fair?
 - Readers are preferred!
 - Can always delay writers (again and again and again)

const W = 1;
const R = 2;
volatile int lock=0; // LSB is writer flag!

void read_lock(lock_t lock) {
 AtomicAdd(lock, R);
 while(lock & W);
}

void write_lock(lock_t lock) {
 while(!CAS(lock, 0, W));
}

void read_unlock(lock_t lock) {
 AtomicAdd(lock, -R);
}

void write_unlock(lock_t lock) {
 AtomicAdd(lock, -W);
}

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Fixing those Issues?

- Polling issue:
 - Combine with MCS lock idea of queue polling
- Fairness:
 - Count readers and writers



Deadlocks

Kansas state legislature: "When two trains approach each other at a crossing, both shall come to a full stop and neither shall start up again until the other has gone."

[according to Botkin, Harlow "A Treasury of Railroad Folklore" (pp. 381)]



What are necessary conditions for deadlock?

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Deadlocks

- Necessary conditions:
 - Mutual Exclusion
 - Hold one resource, request another
 - No preemption
 - Circular wait in dependency graph
- One condition missing will prevent deadlocks!
 - → Different avoidance strategies (which?)

Issues with Spinlocks

- Spin-locking is very wasteful
 - The spinning thread occupies resources
 - Potentially the PE where the waiting thread wants to run → requires context switch!
- Context switches due to
 - Expiration of time-slices (forced)
 - Yielding the CPU

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Why is the 1997 Mars Rover in our lecture?

- It landed, received program, and worked ... until it spuriously rebooted!
 - → watchdog
- Scenario (vxWorks RT OS):
 - Single CPU
 - Two threads A, B sharing common bus, using locks
 - (independent) thread C wrote data to flash
 - Priority: A→C→B (A highest, B lowest)
 - Thread C would run into a lifelock (infinite loop)
 - Thread B was preempted by C while holding lock
 - Thread A got stuck at lock ⊗

[http://research.microsoft.com/en-us/um/people/mbj/Mars_Pathfinder/Authoritative_Account.html]

1.4

Priority Inversion

- If busy-waiting thread has higher priority than thread holding lock ⇒ no progress!
- Can be fixed with the help of the OS
 - E.g., mutex priority inheritance (temporarily boost priority of task in CR to highest priority among waiting tasks)

Fighting CPU waste: Condition Variables

- Allow threads to yield CPU and leave the OS run queue
 - Other threads can get them back on the queue!
- cond_wait(cond, lock) yield and go to sleep
- cond_signal(cond) wake up sleeping threads
- Wait and signal are OS calls
 - Often expensive, which one is more expensive?
 Wait, because it has to perform a full context switch

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Condition Variable Semantics

- Hoare-style:
 - Signaler passes lock to waiter, signaler suspended
 - Waiter runs immediately
 - Waiter passes lock back to signaler if it leaves critical section or if it waits again
- Mesa-style (most used):
 - Signaler keeps lock
 - Waiter simply put on run queue
 - Needs to acquire lock, may wait again

When to Spin and When to Block?

- Spinning consumes CPU cycles but is cheap
 - "Steals" CPU from other threads
- Blocking has high one-time cost and is then free
 - Often hundreds of cycles (trap, save TCB ...)
 - Wakeup is also expensive (latency)
 Also cache-pollution
- Strategy:
 - Poll for a while and then block

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When to Spin and When to Block?

- What is a "while"?
- Optimal time depends on the future
 - When will the active thread leave the CR?
 - Can compute optimal offline schedule
 - Q: What is the optimal offline schedule (assuming we know the future, i.e., when the lock will become available)?
 - Actual problem is an online problem
- Competitive algorithms
 - An algorithm is c-competitive if for a sequence of actions x and a constant a holds:

 $C(x) \le c * C_{opt}(x) + a$

What would a good spinning algorithm look like and what is the competitiveness?

Competitive Spinning

- If T is the overhead to process a wait, then a locking algorithm that spins for time T before it blocks is 2-competitive!
 - Karlin, Manasse, McGeoch, Owicki: "Competitive Randomized Algorithms for Non-Uniform Problems", SODA 1989
- If randomized algorithms are used, then e/(e-1)-competitiveness (~1.58) can be achieved
 - See paper above!

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Generalized Locks: Semaphores

- Controlling access to more than one resource
 - Described by Dijkstra 1965
- Internal state is an atomic counter C
- Two operations:
 - P() block until C>0; decrement C (atomically)
 - V() signal and increment C
- Binary or 0/1 semaphore equivalent to lock
 - C is always 0 or 1, i.e., V() will not increase it further
- Trivia:
 - If you're lucky (aehem, speak Dutch), mnemonics:
 Verhogen (increment) and Prolaag (probeer te verlagen = try to reduce)

Semaphore Implementation

- Can be implemented with mutual exclusion!
 - And can be used to implement mutual exclusion ^⑤
- ... or with test and set and many others!
- Also has fairness concepts:
 - Order of granting access to waiting (queued) threads
 - strictly fair (starvation impossible, e.g., FIFO)
 - weakly fair (starvation possible, e.g., random)

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Case Study 1: Barrier

- Barrier semantics:
 - No process proceeds before all processes reached barrier
 - Similar to mutual exclusion but not exclusive, rather "synchronized"
- Often needed in parallel high-performance programming
 - Especially in SPMD programming style
- Parallel programming "frameworks" offer barrier semantics (pthread, OpenMP, MPI)
 - MPI_Barrier() (process-based)
 - pthread_barrier
 - #pragma omp barrier
 - ...
- Simple implementation: lock xadd + spin

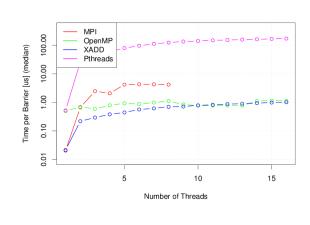
Problem: when to re-use the counter?

Cannot just set it to 0 $\ensuremath{\mathfrak{G}} \to \mathsf{Trick}$: "lock xadd -1" when done $\ensuremath{\mathfrak{G}}$

[cf. http://www.spiral.net/software/barrier.html]

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Barrier Performance



Case Study 2: Reasoning about Semantics

Comments on a Problem in Concurrent Programming Control

Dear Editor

I would like to comment on Mr. Dijkstra's solution [Solution of a problem in concurrent programming control. Comm ACM 8 (Sept. 1965), 569] to a messy problem that is hardly academic. We

are using it now on a multiple computer complex.

When there are only two computers, the algorithm may be simplified to the following:

Boolean array b(0; 1) integer k, i, j, comment This is the program for computer i, which may be either 0 or 1, computer $j \neq i$ is the other one, 1 or 0; C0: b(i): f also, f (2): f (3): f (4): f (5): f (6): f (6): f (6): f (6): f (7): f (8): f (7): f (8): f (8)

go to C0; end

Mr. Dijkstra has come up with a clever solution to a really

HARRIS HYMAN Munitype New York, New York

Volume 9 Issue 1, Jan. 1966

CACM

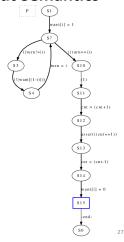
Case Study 2: Reasoning about Semantics

- Is the proposed algorithm correct?
 - We may proof it manually Using tools from the last lecture → reason about the state space of H
 - Or use automated proofs (model checking) E.g., SPIN (Promela syntax)

bool want[2]; bool turn: byte cnt; proctype P(bool i) want[i] = 1; :: (turn != i) -> (!want[1-i]); turn = i :: (turn == i) -> break od; skip; /* critical section */ cnt = cnt+1: assert(cnt == 1); want[i] = 0init { run P(0); run P(1) }

Case Study 2: Reasoning about Semantics

- Spin tells us quickly that it found a problem
 - A sequentially consistent order that violates mutual exclusion!
- It's not always that easy
 - This example comes from the SPIN tutorial
 - More than two threads make it much more demanding!
- More in the recitation!



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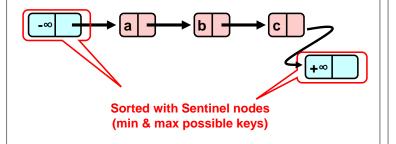
Locks in Practice

- Running example: List-based set of integers
 - S.insert(v) return true if v was inserted
 - S.remove(v) return true if v was removed
 - S.contains(v) return true iff v in S
- Simple ordered linked list
 - Do not use this at home (poor performance)
 - Good to demonstrate locking techniques E.g., skip lists would be faster but more complex

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Set Structure in Memory

This and many of the following illustrations are provided by Maurice Herlihy in conjunction with the book "The Art of Multiprocessor Programming"



Sequential Set

boolean add(S, x) { node *pred = S.head; node *curr = pred.next; while(curr.key < x) { pred = curr; curr = pred.next; if(curr.key == x)return false; node n = new node(); n.next = curr; pred.next = n; return true;

boolean remove(S, x) { node *pred = S.head; node *curr = pred.next; while(curr.key < x) { pred = curr; curr = pred.next; $if(curr.key == x) {$ pred.next = curr.next; free(curr); return true; return false;

boolean contains(S, x) { while(curr.key < x) curr = curr.next; if(curr.key == x) return true; return false;

typedef struct { int key; node *next: } node;

sequential Operations add () remove ()

Concurrent Sets

- What can happen if multiple threads call set operations at the "same time"?
 - Operations can conflict!
- Which operations conflict?
 - (add, remove), (add, add), (remove, remove), (remove, contains) will conflict
 - (add, contains) may miss update (which is fine)
 - (contains, contains) does not conflict
- How can we fix it?

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Coarse-grained Locking

boolean add(S, x) { node *pred = S.head; node *curr = pred.next; while(curr.key < x) { pred = curr; curr = pred.next; if(curr.key == x)unlock(S return false; else { node node = malloc(); node.key = x;node.next = curr; pred.next = node; unlock(S); return true;

boolean remove(S, x) {
 lock(S);
 node *pred = S.head;
 node *curr = pred.next;
 while(curr.key < x) {
 pred = curr;
 curr = pred.next;
 }
 if(curr.key == x) {
 pred.next = curr.next;
 unlock(S);
 free(curr);
 return true;
 }
 unlock(S);
 return false;

boolean contains(S, x) {
 lock(S);
 int *curr = S.head;
 while(curr.key < x)
 curr = curr.next;
 if(curr.key == x) {
 unlock(S);
 return true;
 }
 unlock(S);
 return false;
}

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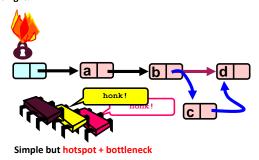
Coarse-grained Locking

- Correctness proof?
 - Assume sequential version is correct
 Alternative: define set of invariants and proof that initial condition as well as all transformations adhere (pre- and post conditions)
 - Proof that all accesses to shared data are in CRs
 This may prevent some optimizations
- Is the algorithm deadlock-free? Why?
 - Locks are acquired in the same order (only one lock)
- Is the algorithm starvation-free and/or fair? Why?
 - It depends on the properties of the used locks!

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Coarse-grained Locking

Is the algorithm performing well with many concurrent threads accessing it?



Coarse-grained Locking

- Is the algorithm performing well with many concurrent threads accessing it?
 - No, access to the whole list is serialized
- BUT: it's easy to implement and proof correct
 - Those benefits should never be underestimated
 - May be just good enough
 - "We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil. Yet we should not pass up our opportunities in that critical 3%. A good programmer will not be lulled into complacency by such reasoning, he will be wise to look carefully at the critical code; but only after that code has been identified" — Donald Knuth (in Structured Programming with Goto Statements)

How to Improve?

- Will present some "tricks"
 - Apply to the list example
 - But often generalize to other algorithms
 - Remember the trick, not the example!
- See them as "concurrent programming patterns" (not literally)
 - Good toolbox for development of concurrent programs
 - They become successively more complex

Tricks Overview

- Fine-grained locking
 - Split object into "lockable components"
 - Guarantee mutual exclusion for conflicting accesses to same component
- 2. Reader/writer locking
- 3. Optimistic synchronization
- 4. Lazy locking
- Lock-free

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Tricks Overview

- 1. Fine-grained locking
- 2. Reader/writer locking
 - Multiple readers hold lock (traversal)
 - contains() only needs read lock
 - Locks may be upgraded during operation
 Must ensure starvation-freedom for writer locks!
- 3. Optimistic synchronization
- 4. Lazy locking
- 5. Lock-free

Tricks Overview

- Fine-grained locking
- 2. Reader/writer locking
- 3. Optimistic synchronization
 - Traverse without locking Need to make sure that this is correct!
 - Acquire lock if update necessary
 May need re-start from beginning, tricky
- Lazy locking
- 5. Lock-free

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Tricks Overview

- 1. Fine-grained locking
- 2. Reader/writer locking
- 3. Optimistic synchronization
- 4. Lazy locking
 - Postpone hard work to idle periods
 - Mark node deleted
 Delete it physically later
- 5. Lock-free

Tricks Overview

- 1. Fine-grained locking
- 2. Reader/writer locking
- 3. Optimistic synchronization
- 4. Lazy locking
- 5. Lock-free
 - Completely avoid locks
 - Enables wait-freedom
 - Will need atomics (see later why!)
 - Often very complex, sometimes higher overhead

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Trick 1: Fine-grained Locking

- Each element can be locked
 - High memory overhead
 - Threads can traverse list concurrently like a pipeline

Tricky to prove correctness

- And deadlock-freedom
- Two-phase locking (acquire, release) often helps
- Hand-over-hand (coupled locking)
 - Not safe to release x's lock before acquiring x.next's lock will see why in a minute

typedef struct {
 int key;
 node *next;
 lock_t lock;

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} node;

Important to acquire locks in the same order

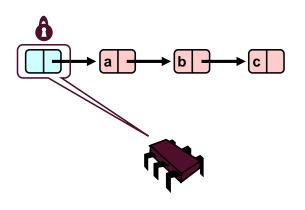
Hand-over-Hand (fine-grained) locking



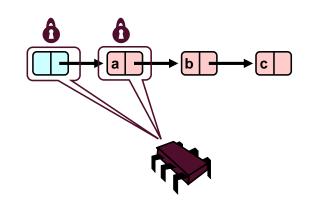


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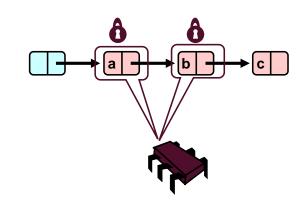
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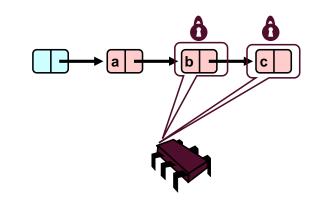
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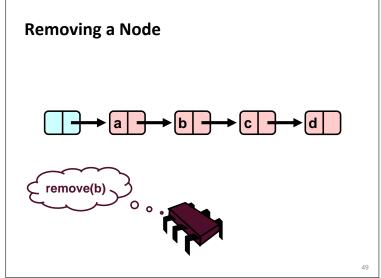


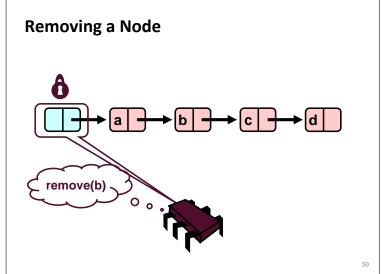
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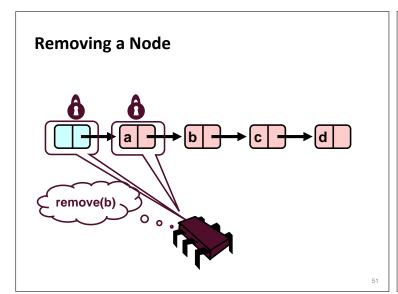


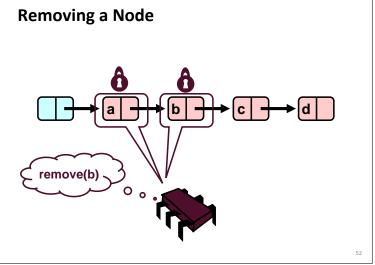
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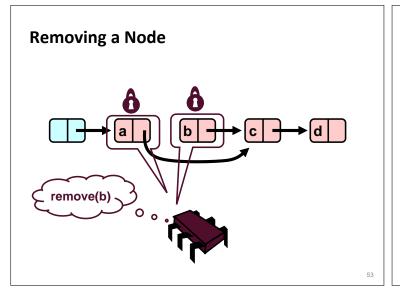


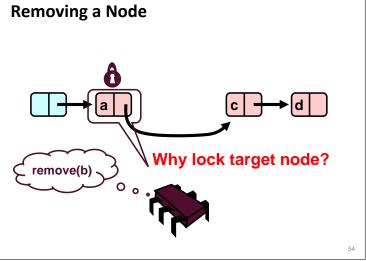


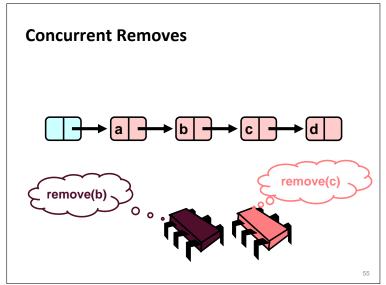


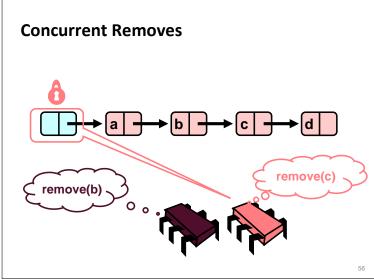


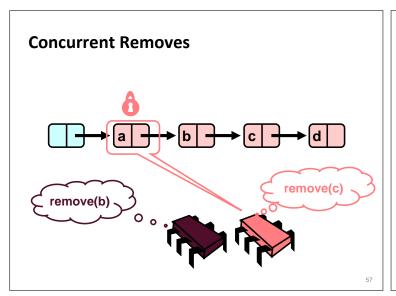


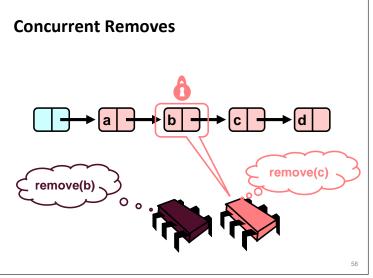


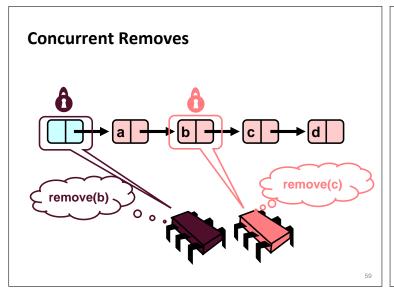


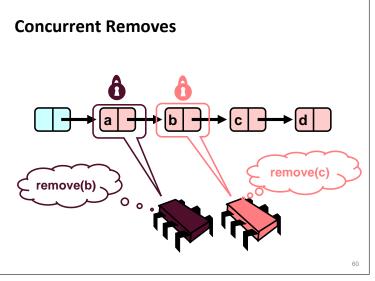


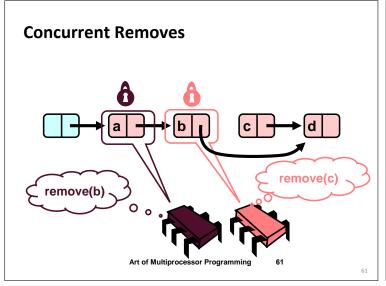


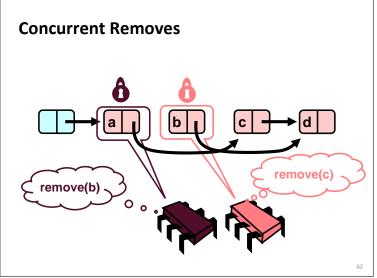


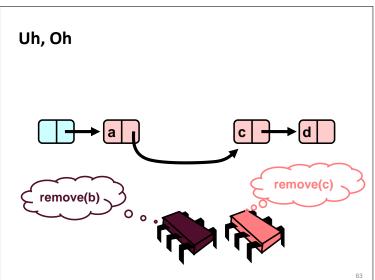


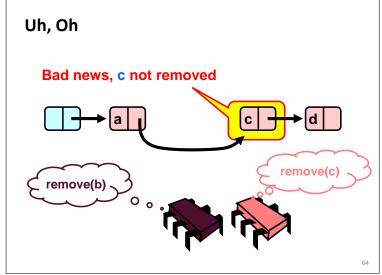






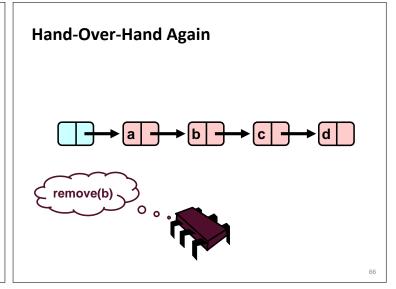


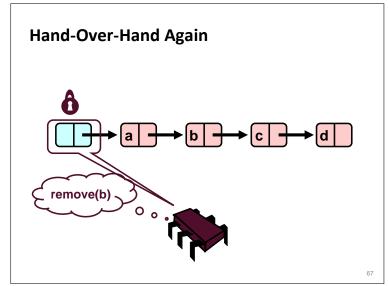


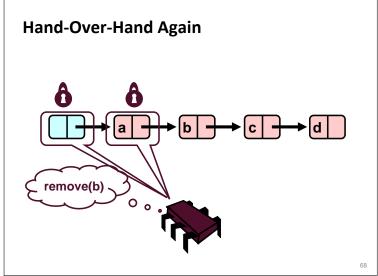


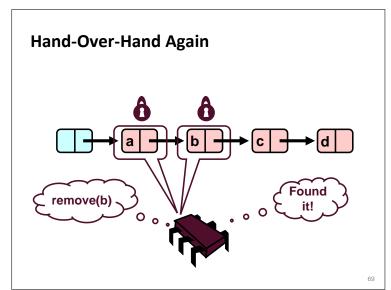
Insight

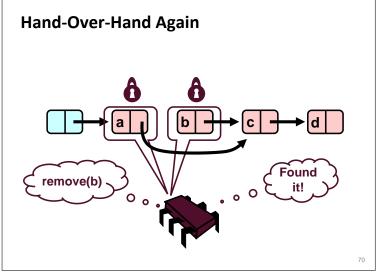
- If a node x is locked
 - Successor of x cannot be deleted!
- Thus, safe locking is
 - Lock node to be deleted
 - And its predecessor!
 - → hand-over-hand locking

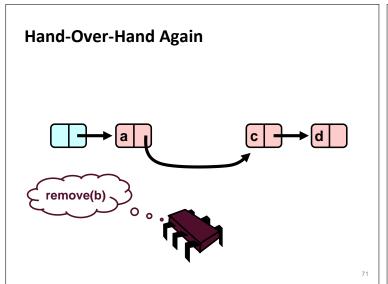


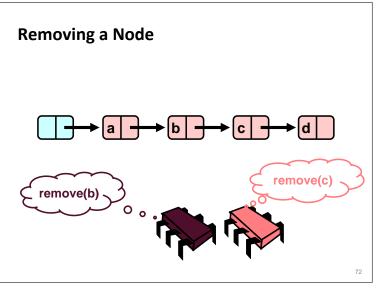


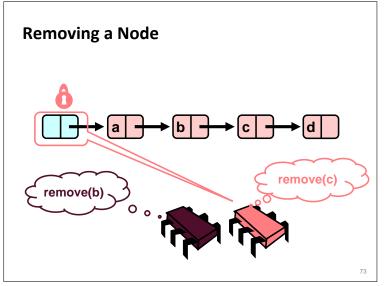


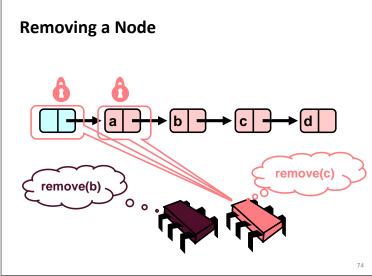


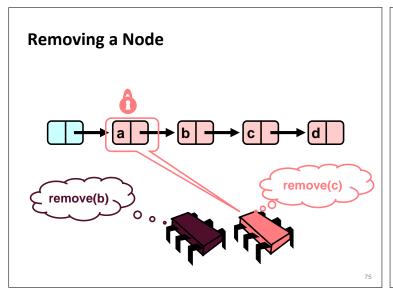


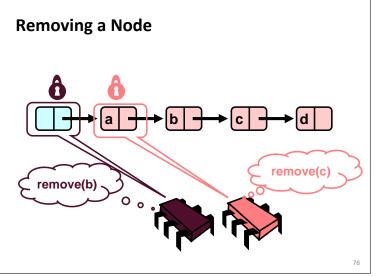


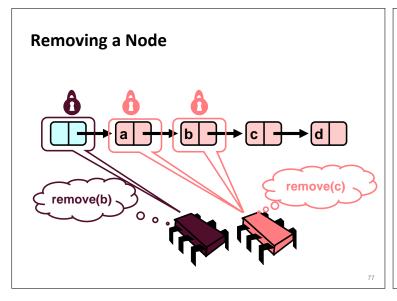


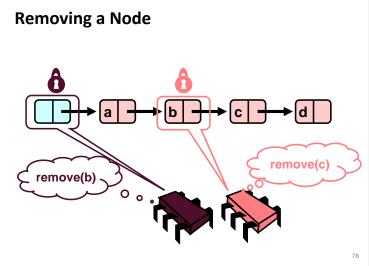


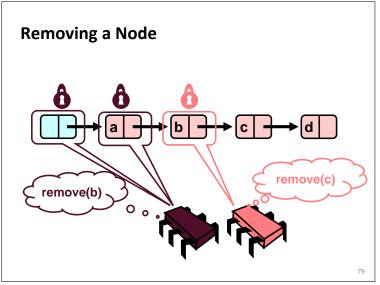


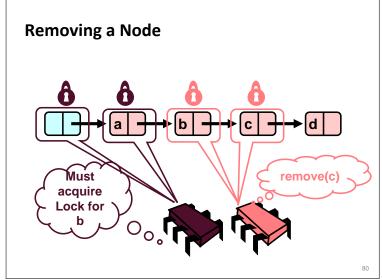


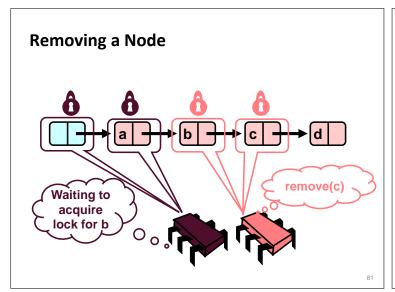


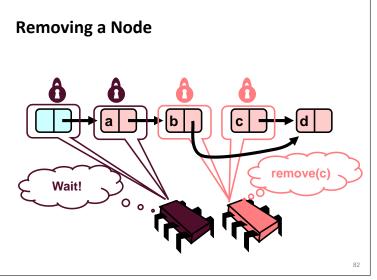


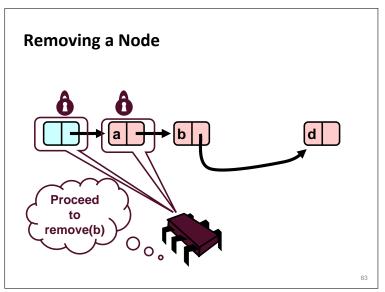


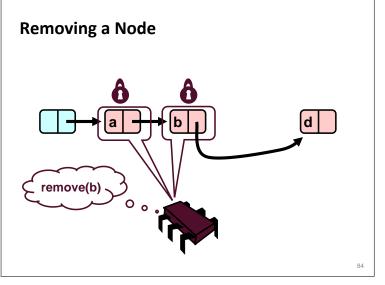


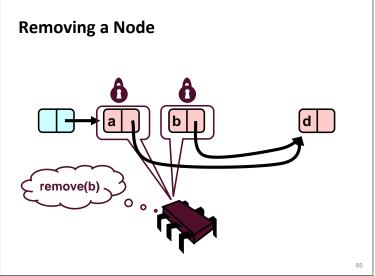


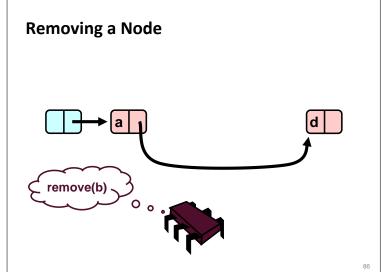












What are the Issues?

- We have fine-grained locking, will there be contention?
 - Yes, the list can only be traversed sequentially, a remove of the 3rd item will block all other threads!
 - This is essentially still serialized if the list is short (since threads can only pipeline on list elements)
- Other problems, ignoring contention?
 - Must acquire O(|S|) locks

Trick 2: Reader/Writer Locking

- Same hand-over-hand locking
 - Traversal uses reader locks
 - Once add finds position or remove finds target node, upgrade both locks to writer locks
 - Need to guarantee deadlock and starvation freedom!
- Allows truly concurrent traversals
 - Still blocks behind writing threads
 - Still O(|S|) lock/unlock operations

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Trick 3: Optimistic synchronization

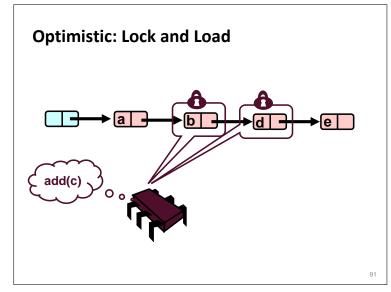
- Similar to reader/writer locking but traverse list without locks
 - Dangerous! Requires additional checks.
- Harder to proof correct

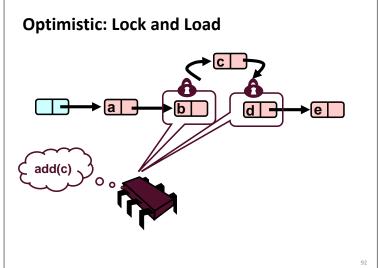
a b d e

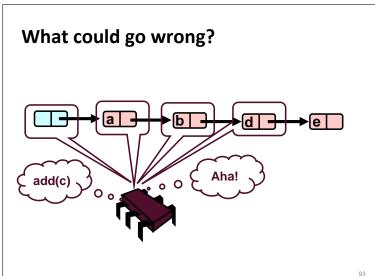
Optimistic: Traverse without Locking

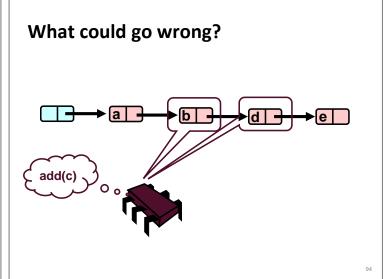
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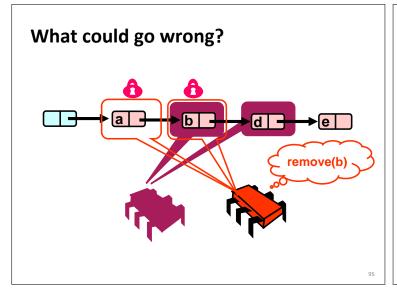
add(c)

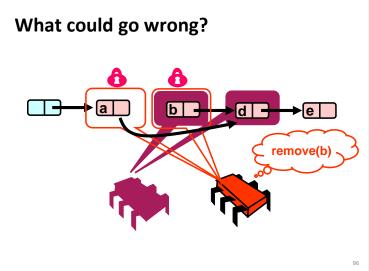


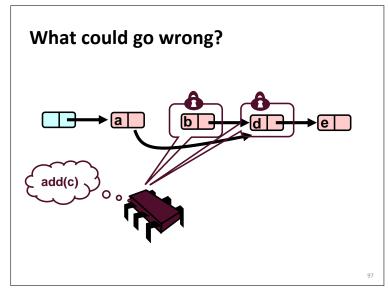


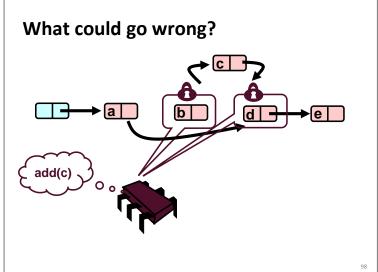


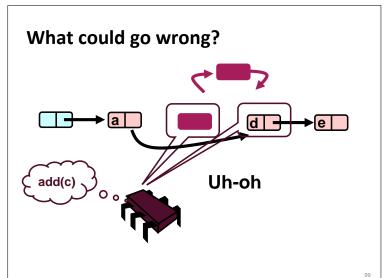


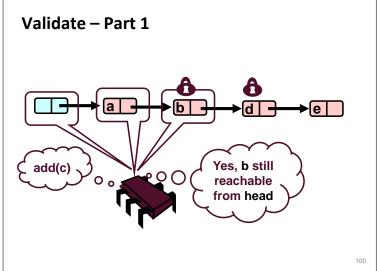


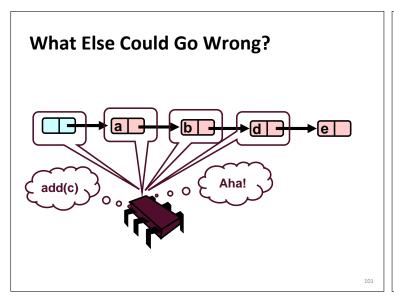


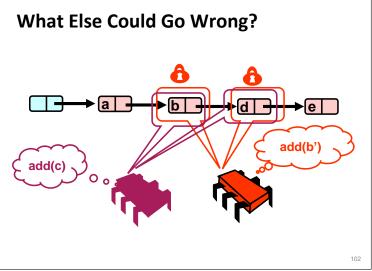


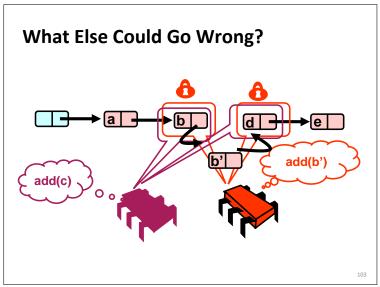


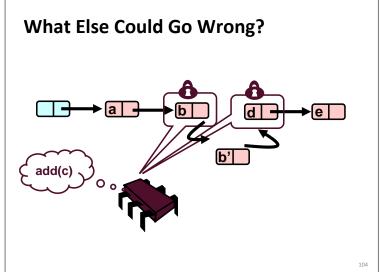


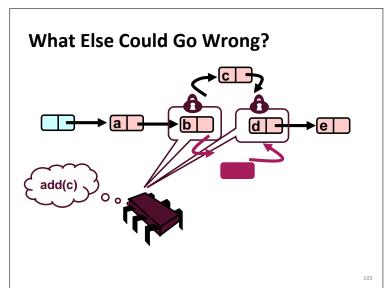


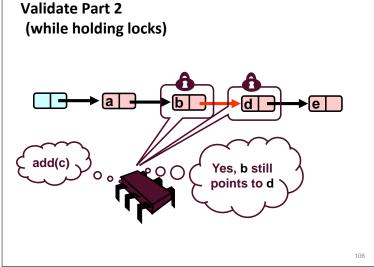












Optimistic synchronization

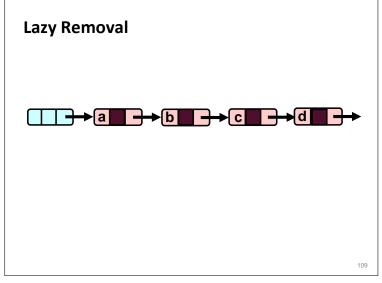
- One MUST validate AFTER locking
 - 1. Check if the path how we got there is still valid!
 - 2. Check if locked nodes are still connected
 - If any of those checks fail?
 Start over from the beginning (hopefully rare)
- Not starvation-free
 - A thread may need to abort forever if nodes are added/removed
 - Should be rare in practice!
- Other disadvantages?
 - All operations require two traversals of the list!
 - Even contains() needs to check if node is still in the list!

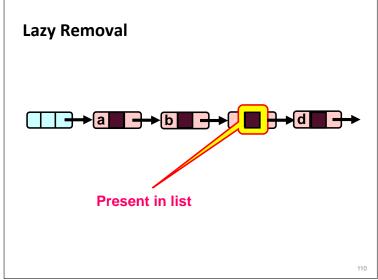
Trick 4: Lazy synchronization

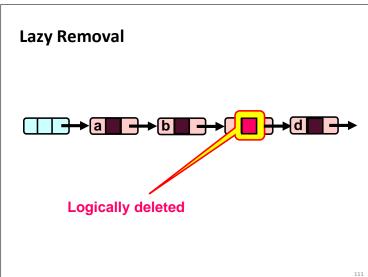
- We really want one list traversal
- Also, contains() should be wait-free
 - Is probably the most-used operation
- Lazy locking is similar to optimistic
 - Key insight: removing is problematic
 - Perform it "lazily"
- Add a new "valid" field
 - Indicates if node is still in the set
 - Can remove it without changing list structure!
 - Scan once, contains() never locks!

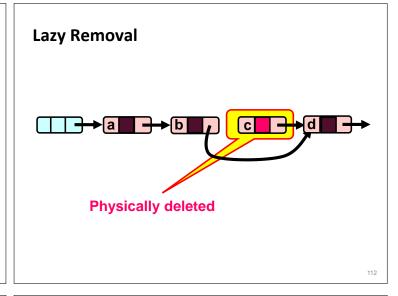
typedef struct {
 int key;
 node *next;
 lock_t lock;
 boolean valid;
} node;

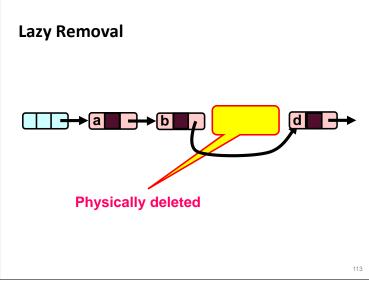
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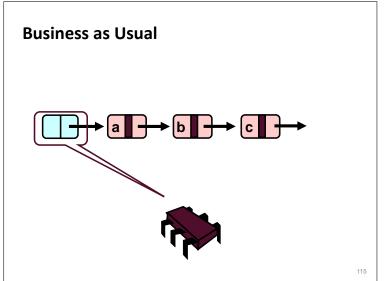


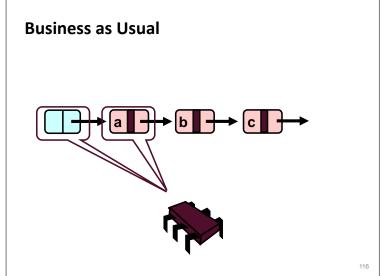


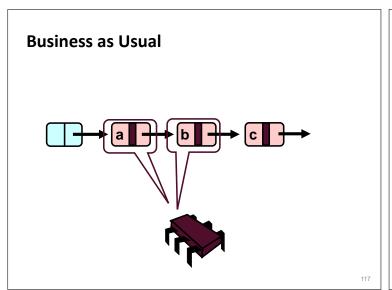


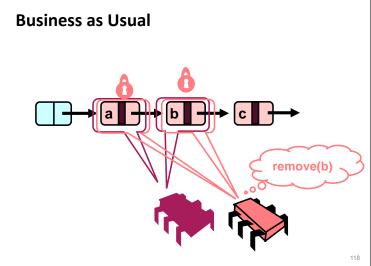
How does it work?

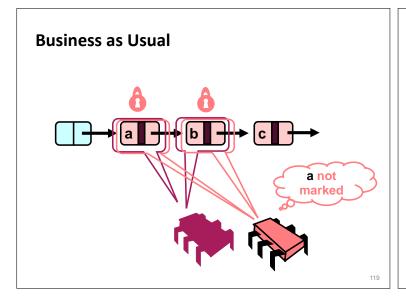
- Eliminates need to re-scan list for reachability
 - Maintains invariant that every **unmarked** node is reachable!
- Contains can now simply traverse the list
 - Just check marks, not reachability, no locks
- Remove/Add
 - Scan through locked and marked nodes
 - Removing does not delay others
 - Must only lock when list structure is updated
 Check if neither pred nor curr are marked, pred.next == curr

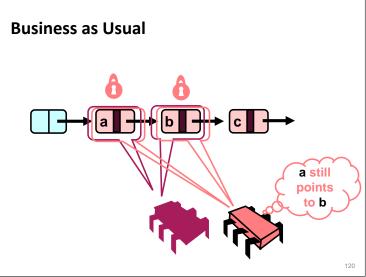


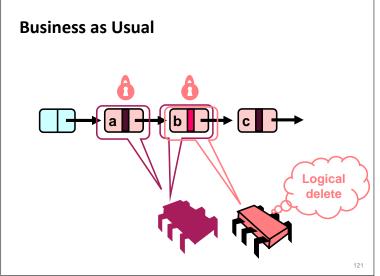


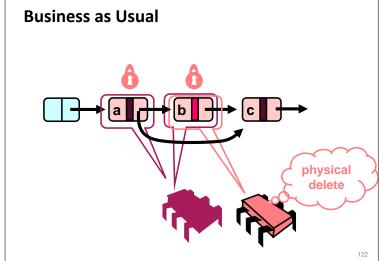


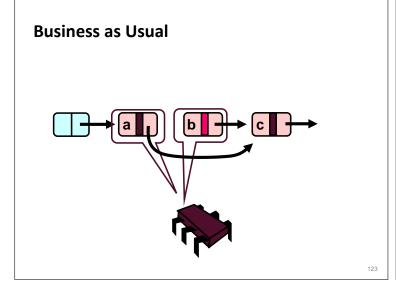


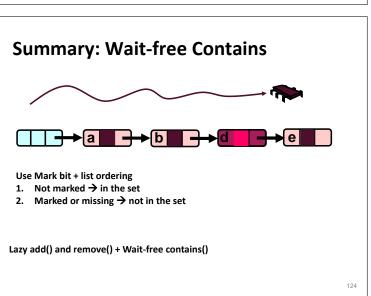












Problems with Locks

- What are the fundamental problems with locks?
- Blocking
 - Threads wait, fault tolerance
 - Especially when things like page faults occur in CR
- Overheads
 - Even when not contended
 - Also memory/state overhead
- Synchronization is tricky
 - Deadlock, other effects are hard to debug
- Not easily composable

Lock-free Methods

- No matter what:
 - Guarantee minimal progress
 - I.e., some thread will advance
 - Threads may halt at bad times (no CRs! No exclusion!)
 - I.e., cannot use locks!
 - Needs other forms of synchronization
 - E.g., atomics (discussed before for the implementation of locks)
 Techniques are astonishingly similar to guaranteeing mutual exclusion

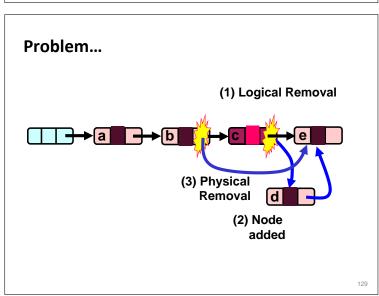
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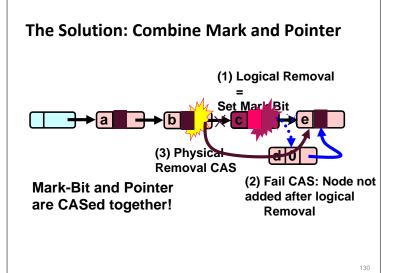
Trick 5: No Locking

- Make list lock-free
- Logical succession
 - We have wait-free contains
 - Make add() and remove() lock-free! Keep logical vs. physical removal
- Simple idea:
 - Use CAS to verify that pointer is correct before moving it

Use CAS to verify pointer is correct
Not enough! Why?

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Practical Solution(s)

- Option 1:
 - Introduce "atomic markable reference" type
 - "Steal" a bit from a pointer
 - \blacksquare Rather complex and OS specific $\ensuremath{\mathfrak{S}}$
- Option 2
 - Use Double CAS (or CAS2) ⁽²⁾

 CAS of two noncontiguous locations
 - Well, not many machines support it Any still alive?
- Option 3:
 - Our "favorite" ISA (x86) offers double-width CAS Contiguous, e.g., lock cmpxchg16b (on 64 bit systems)
- Option 4
 - Transactional Memory!

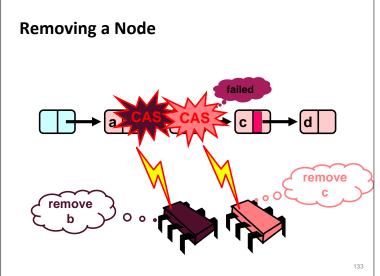
E.g., Intel's TSX (essentially a cmpxchg64b (operates on a cache line))

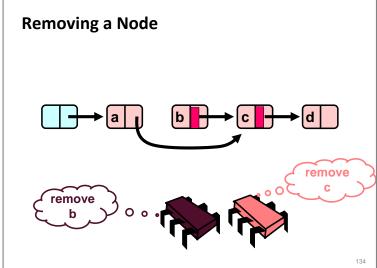
Removing a Node

Temove

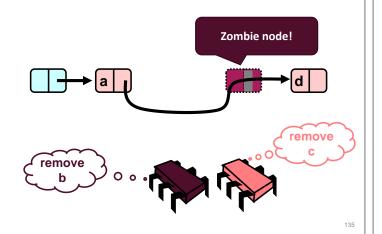
Tremove

Table 132





Uh oh – node marked but not removed!



Dealing With Zombie Nodes

- Add() and remove() "help to clean up"
 - Physically remove any marked nodes on their path
 - I.e., if curr is marked: CAS (pred.next, mark) to (curr.next, false) and remove curr

If CAS fails, restart from beginning!

- "Helping" is often needed in wait-free algs
- This fixes all the issues and makes the algorithm correct!

Comments

- Atomically updating two variables (CAS2 etc.) has a non-trivial cost
- If CAS fails, routine needs to re-traverse list
 - Necessary cleanup may lead to unnecessary contention at marked nodes
- More complex data structures and correctness proofs than for locked versions
 - But guarantees progress, fault-tolerant and maybe even faster (that really depends)

More Comments

- Correctness proof techniques
 - Establish invariants for initial state and transformations
 E.g., head and tail are never removed, every node in the set has to be reachable from head, ...
 - Proofs are similar to those we discussed for locks
 Very much the same techniques (just trickier)
 Using sequential consistency (or consistency model of your choice @)
 Lock-free gets somewhat tricky
- Source-codes can be found in Chapter 9 of "The Art of Multiprocessor Programming"

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Defining lock-free and wait-free

- A lock-free method
 - guarantees that infinitely often some method call finishes in a finite number of steps
- - guarantees that each method call finishes in a finite number of steps (implies lock-free)
- Synchronization instructions are not equally powerful!
 - Indeed, they form an infinite hierarchy; no instruction (primitive) in level x can be used for lock-/wait-free implementations of primitives in level z>x.

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Concept: Consensus Number



- Each level of the hierarchy has a "consensus number" assigned.
 - Is the maximum number of threads for which primitives in level x can solve the consensus problem
- The consensus problem:
 - Has single function: decide(v)
 - Each thread calls it at most once, the function returns a value that meets two
 - consistency: all threads get the same value validity: the value is some thread's input
 - Simplification: binary consensus (inputs in {0,1})

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Understanding Consensus

- Can a particular class solve n-thread consensus wait-free?
 - A class C solves n-thread consensus if there exists a consensus protocol using any number of objects of class C and any number of atomic registers
 - The protocol has to be wait-free (bounded number of steps per thread)
 - The consensus number of a class C is the largest n for which that class solves n-thread consensus (may be infinite)
 - Assume we have a class D whose objects can be constructed from objects out of class C. If class C has consensus number n, what does class D have?

Starting simple ...

- Binary consensus with two threads (A, B)!
 - Each thread moves until it decides on a value
 - May update shared objects
 - Protocol state = state of threads + state of shared objects
 - Initial state = state before any thread moved
 - Final state = state after all threads finished
 - States form a tree, wait-free property guarantees a finite tree Example with two threads and two moves each!

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Atomic Registers

- Theorem [Herlihy'91]: Atomic registers have consensus number one
 - I.e., they cannot be used to solve even two-thread consensus! Really?
- Proof outline:
 - Assume arbitrary consensus protocol, thread A, B
 - Run until it reaches critical state where next action determines outcome (show that it must have a critical state first)
 - Show all options using atomic registers and show that they cannot be used to determine one outcome for all possible executions!
 - 1) Any thread reads (other thread runs solo until end)
 - 2) Threads write to different registers (order doesn't matter)
 - Threads write to same register (solo thread can start after each

Atomic Registers

- Theorem [Herlihy'91]: Atomic registers have consensus number one
- Corollary: It is impossible to construct a wait-free implementation of any object with consensus number of >1 using atomic registers
 - "perhaps one of the most striking impossibility results in Computer Science" (Herlihy, Shavit)
 - ightarrow We need hardware atomics or Transactional Memory!
- Proof technique borrowed from:

Impossibility of distributed consensus with one ... - ACM Digita... di.acm.org/citation.cfm?d=214121 ▼
by MJ Fischer - 1985 - Cited by 4189 - Related articles
Apr 1, 1985 - The consensus problem involves an asynchronous
some of which may be unreliable. The problem is for the reliable.

- Very influential paper, always worth a read!
 - Nicely shows proof techniques that are central to parallel and distributed

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Other Atomic Operations

- Simple RMW operations (Test&Set, Fetch&Op, Swap, basically all functions where the op commutes or overwrites) have consensus number 2!
 - Similar proof technique (bivalence argument)
- CAS and TM have consensus number ∞
 - Constructive proof!

Compare and Set/Swap Consensus

volatile int thread = -1; int proposed[n]; int decide(v) { proposed[tid] = v; if(CAS(thread, first, tid)) return v; // I won! return proposed[thread]; // thread won



- CAS provides an infinite consensus number
 - Machines providing CAS are asynchronous computation equivalents of the
 - I.e., any concurrent object can be implemented in a wait-free manner (not necessarily fast!)

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Now you know everything ⁽²⁾

- Not really ... ;-)
 - We'll argue more about **performance** now!
- But you have all the tools for:

 - Efficient lock-based algorithms
 - Efficient lock-free algorithms (or even wait-free)
 - Reasoning about parallelism!
- What now?
 - A different class of problems

Impact on wait-free/lock-free on actual performance is not well understood

 Relevant to HPC, applies to shared and distributed memory → Group communications

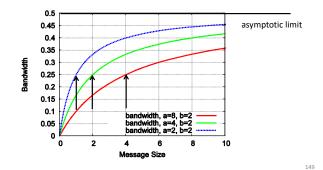
Remember: A Simple Model for Communication

- Transfer time $T(s) = \alpha + \beta s$
 - α = startup time (latency)
 - $\beta = \cos \beta$ per byte (bandwidth=1/ β)
- As s increases, bandwidth approaches 1/β asymptotically
 - \blacksquare Convergence rate depends on α
 - $s_{1/2} = \alpha/\beta$
- Assuming no pipelining (new messages can only be issued from a process after all arrived)

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Bandwidth vs. Latency

- $s_{1/2} = \alpha/\beta$ often used to distinguish bandwidth- and latencybound messages
 - s_{1/2} is in the order of kilobytes on real systems



Quick Example

- Simplest linear broadcast
 - One process has a data item to be distributed to all processes
- Broadcasting s bytes among P processes:
 - T(s) = (P-1) * (α + β s) = $\mathcal{O}(P)$
- Class question: Do you know a faster method to accomplish the same?

k-ary Tree Broadcast

- Origin process is the root of the tree, passes messages to k neighbors which pass them on
 - k=2 -> binary tree
- Class Question: What is the broadcast time in the simple latency/bandwidth model?
 - $T(s) \approx \lceil log_k(P) \rceil \cdot k \cdot (\alpha + \beta \cdot s) = \mathcal{O}(log(P))$ (for fixed k)
- Class Question: What is the optimal k?

•
$$0 = \frac{ln(P) \cdot k}{ln(k)} \frac{d}{dk} = \frac{ln(P) ln(k) - ln(P)}{ln^2(k)} \rightarrow k = e = 2.71...$$

• Independent of P, α, βs? Really?

Faster Trees?

- Class Question: Can we broadcast faster than in a ternary tree?
 - Yes because each respective root is idle after sending three messages!
 - Those roots could keep sending!
 - Result is a k-nomial tree
 For k=2, it's a binomial tree
- Class Question: What about the runtime?

$$T(s) = \lceil \log_k(P) \rceil \cdot (k-1) \cdot (\alpha + \beta \cdot s) = \mathcal{O}(\log(P))$$

- Class Question: What is the optimal k here?
 - T(s) d/dk is monotonically increasing for k>1, thus k_{opt}=2
- Class Question: Can we broadcast faster than in a k-nomial tree?
 - $lacksquare \mathcal{O}(log(P))$ is asymptotically optimal for s=1!
 - But what about large s?

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Open Problems

- Look for optimal parallel algorithms (even in simple models!)
 - And then check the more realistic models
 - Useful optimization targets are MPI collective operations
 Broadcast/Reduce, Scatter/Gather, Alltoall, Allreduce, Allgather, Scan/Exscan, ...
 - Implementations of those (check current MPI libraries ⑤)
 - Useful also in scientific computations
 Barnes Hut, linear algebra, FFT, ...
- Lots of work to do!
 - Contact me for thesis ideas (or check SPCL) if you like this topic
 - Usually involve optimization (ILP/LP) and clever algorithms (algebra) combined with practical experiments on large-scale machines (10,000+ processors)

HPC Networking Basics

- Familiar (non-HPC) network: Internet TCP/IP
 - Common model:



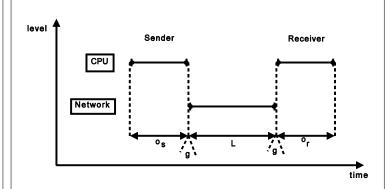
- Class Question: What parameters are needed to model the performance (including pipelining)?
 - Latency, Bandwidth, Injection Rate, Host Overhead

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The LogP Model

- Defined by four parameters:
 - L: an upper bound on the latency, or delay, incurred in communicating a message containing a word (or small number of words) from its source module to its target module.
 - o: the overhead, defined as the length of time that a processor is engaged in the transmission or reception of each message; during this time, the processor cannot perform other operations.
 - g: the gap, defined as the minimum time interval between consecutive message transmissions or consecutive message receptions at a processor. The reciprocal of g corresponds to the available per-processor communication bandwidth.
 - P: the number of processor/memory modules. We assume unit time for local operations and call it a cycle.

The LogP Model



Simple Examples

- Sending a single message
 - T = 2o+L
- Ping-Pong Round-Trip
 - T_{RTT} = 4o+2L
- Transmitting n messages
 - T(n) = L+(n-1)*max(g, o) + 2o

Simplifications

- o is bigger than g on some machines
 - g can be ignored (eliminates max() terms)
 - be careful with multicore!
- Offloading networks might have very low o
 - Can be ignored (not yet but hopefully soon)
- L might be ignored for long message streams
 - If they are pipelined
- Account g also for the first message
 - Eliminates "-1"

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Benefits over Latency/Bandwidth Model

- Models pipelining
 - L/g messages can be "in flight"
 - Captures state of the art (cf. TCP windows)
- Models computation/communication overlap
 - Asynchronous algorithms
- Models endpoint congestion/overload
 - Benefits balanced algorithms

Example: Broadcasts

- Class Question: What is the LogP running time for a linear broadcast of a single packet?
 - T_{lin} = L + (P-2) * max(o,g) + 2o
- Class Question: Approximate the LogP runtime for a binary-tree broadcast of a single packet?
 - $T_{bin} \le log_2 P * (L + max(o,g) + 2o)$
- Class Question: Approximate the LogP runtime for an k-ary-tree broadcast of a single packet?
 - $T_{k-n} \le log_k P * (L + (k-1)max(o,g) + 2o)$

Example: Broadcasts

- Class Question: Approximate the LogP runtime for a binomial tree broadcast of a single packet (assume L > g!)?
 - T_{bin} ≤ log₂P * (L + 2o)
- Class Question: Approximate the LogP runtime for a k-nomial tree broadcast of a single packet?
 - $T_{k-n} \le log_k P * (L + (k-2)max(o,g) + 2o)$
- Class Question: What is the optimal k (assume o>g)?
 - Derive by k: $0 = o * ln(k_{opt}) L/k_{opt} + o$ (solve numerically) For larger L, k grows and for larger o, k shrinks
 - Models pipelining capability better than simple model!

Example: Broadcasts

- Class Question: Can we do better than k_{opt}-ary binomial broadcast?
 - Problem: fixed k in all stages might not be optimal
 - We can construct a schedule for the optimal broadcast in practical settings
 - First proposed by Karp et al. in "Optimal Broadcast and Summation in the LogP Model"

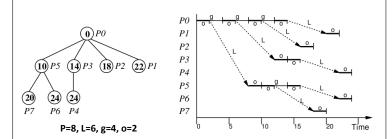
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Example: Optimal Broadcast

- Broadcast to P-1 processes
 - Each process who received the value sends it on; each process receives exactly once



Optimal Broadcast Runtime

- This determines the maximum number of PEs (P(t)) that can be reached in time t
- P(t) can be computed with a generalized Fibonacci recurrence (assuming o>g):

$$P(t) = \begin{cases} 1: & t < 2o + L \\ P(t-o) + P(t-L-2o): & \text{otherwise.} \end{cases}$$
 (1)

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- lacksquare Which can be bounded by (see [1]): $2^{\left\lfloor rac{t}{L+2o}
 ight
 floor} \leq P(t) \leq 2^{\left\lfloor rac{t}{o}
 ight
 floor}$
 - A closed solution is an interesting open problem!

[1]: Hoefler et al.: "Scalable Communication Protocols for Dynamic Sparse Data Exchange" (Lemma 1)

The Bigger Picture

- We learned how to program shared memory systems
 - Coherency & memory models & linearizability
 - Locks as examples for reasoning about correctness and performance
 - List-based sets as examples for lock-free and wait-free algorithms
 - Consensus number
- We learned about general performance properties and parallelism
 - Amdahl's and Gustafson's laws
 - Little's law, Work-span, ...
 - Balance principles & scheduling
- We learned how to perform model-based optimizations
 - Distributed memory broadcast example with two models
- What next? MPI? OpenMP? UPC?
 - Next-generation machines "merge" shared and distributed memory concepts → Partitioned Global Address Space (PGAS)

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